

# Computational approaches for guiding rational vaccine design: Case studies in HCV, HIV, and COVID-19

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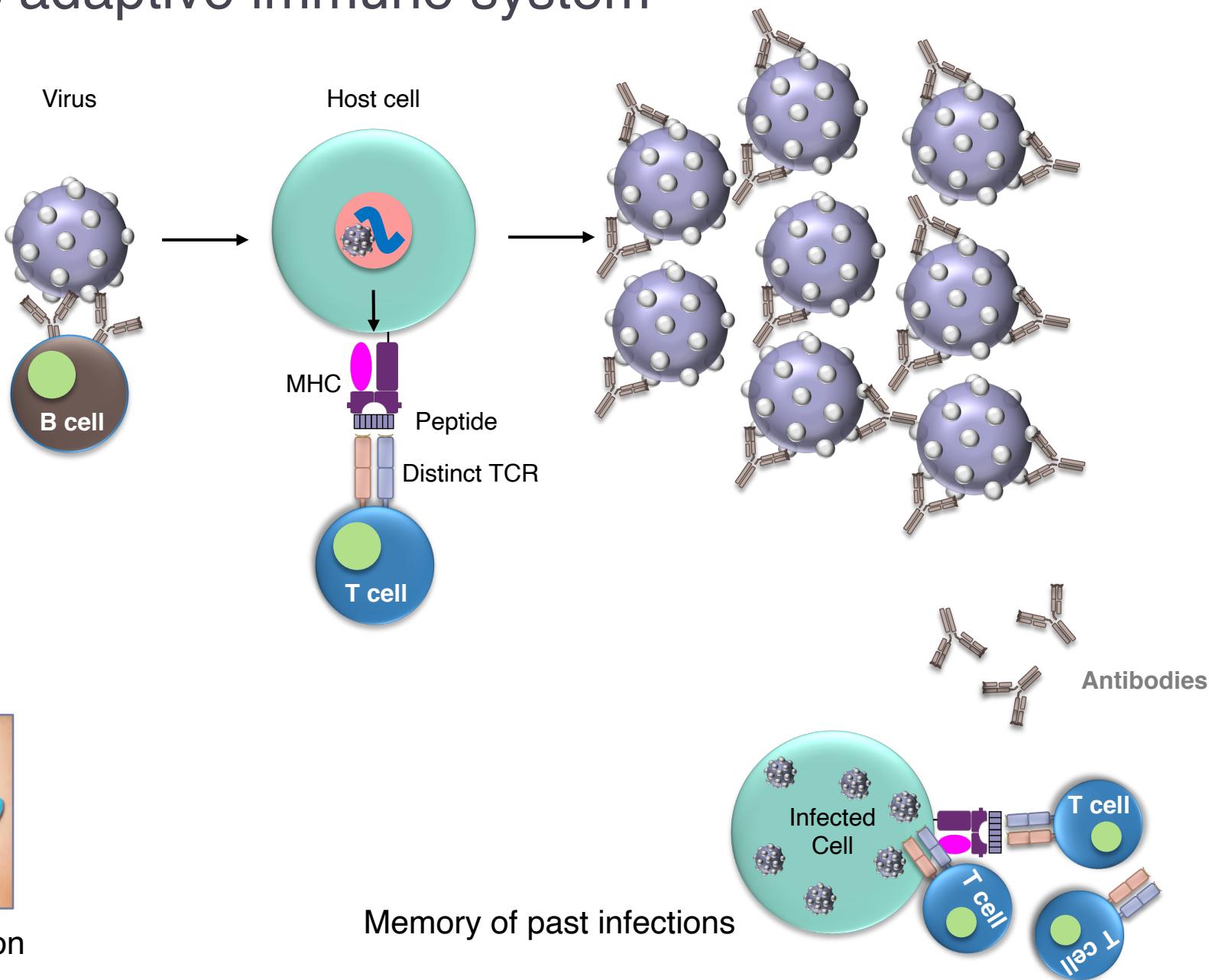
Department of Chemical and Biological Engineering

June 12, 2020, One World Signal Processing Seminar Series

# Pathogen specific adaptive immune system



Basis for vaccination



# Vaccination

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- ▶ Eradication or near-eradication of diseases such as smallpox and polio
- ▶ Still no effective vaccine against many pathogens
- ▶ Main focus of today's talk: **Hepatitis C virus (HCV), SARS-CoV-2, and a bit about HIV**

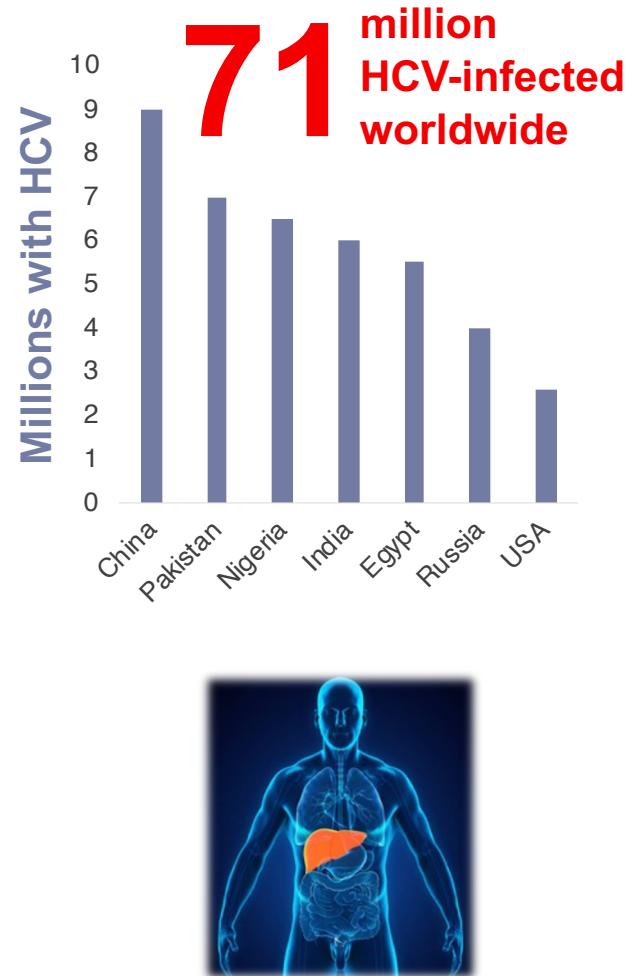
.... and ...

**How data analytics, modelling, and statistical inference can help?**

# PART 1: Identifying escape- resistant antibodies for guiding HCV vaccine design

# Hepatitis C virus

- ▶ Global public health problem
- ▶ Around 20–30% of infections are asymptomatic and resolve within 6 months
- ▶ A leading cause of liver transplants and liver cancer
- ▶ Key challenges in HCV vaccine development:
  - ▶ High replication rate ( $\sim 10^{12}$  copies per day)
  - ▶ High mutation rate ( $\sim 10^{-4}$  mutations/nucleotidereplication cycle)
- ▶ Effective new drugs available, but problem still not fully solved
- ▶ Widespread vaccination would play a key role in eradicating HCV



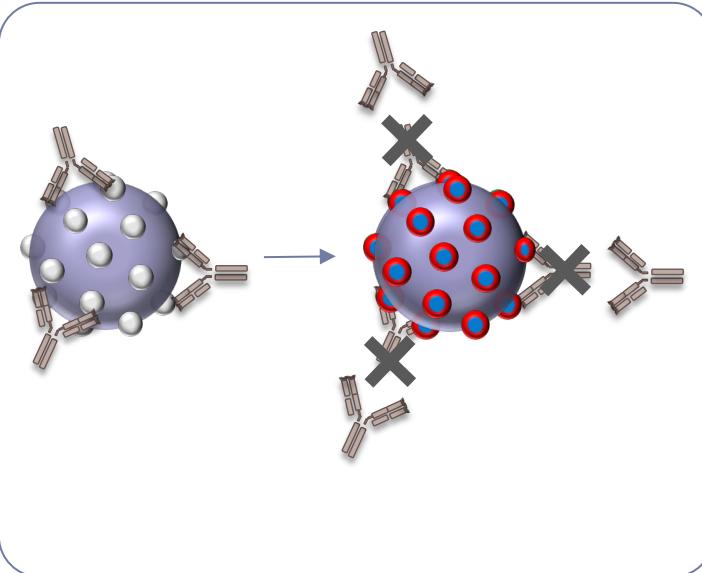
# Immune system evasion by HCV

**Key Point:** Mutations generally do **not** act independently

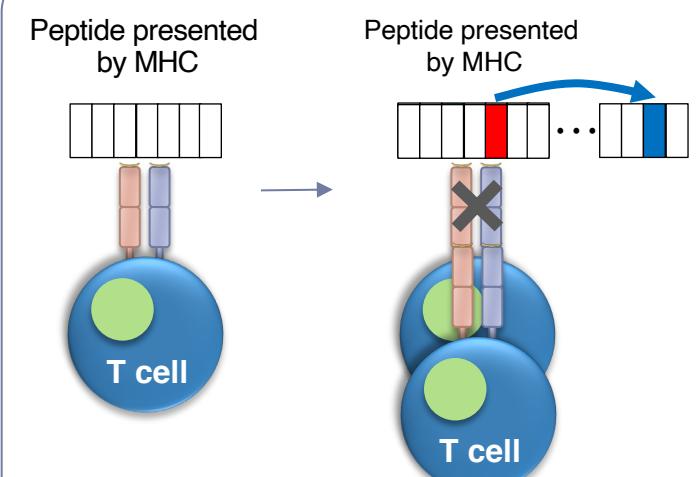
...MRTAPCEWASDEGSFTNPARC...

↓

...MRTAPC**Q****P**AASDEGSFTNP**A**C...



HCV mutation during replication



High mutation rate of HCV results in immune escape if the mutant virus has a **high fitness**

**Additional complication**  
**Compensation** of **deleterious** effect of individual mutations

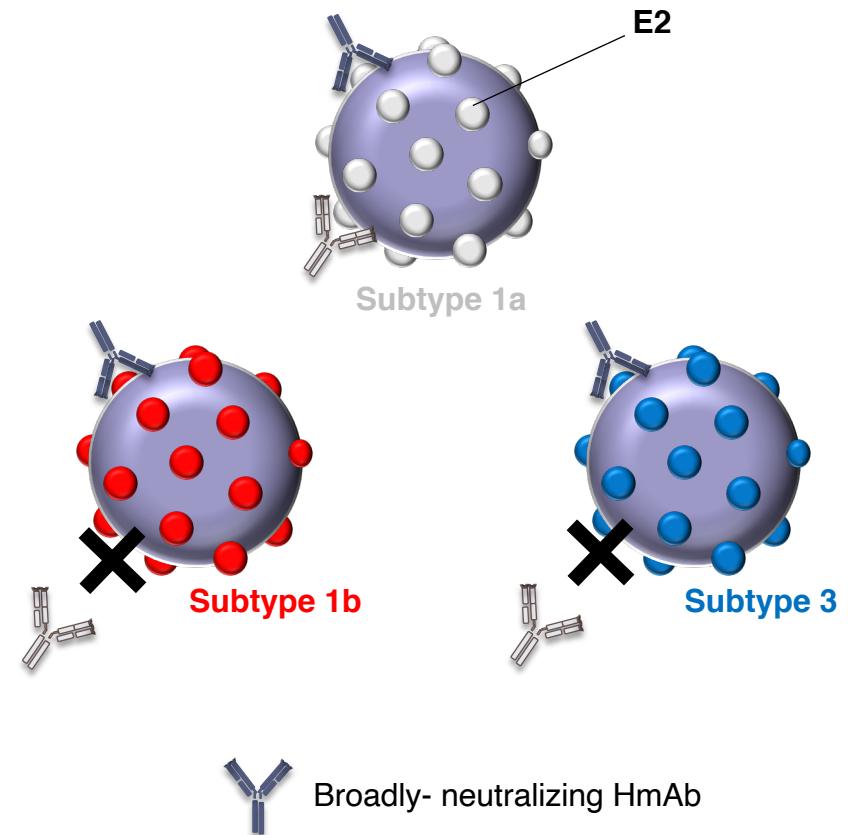
# Problem statement

- ▶ **E2-specific broadly neutralizing human monoclonal antibodies (HmAbs) have been identified for HCV**
  - ▶ Spontaneous clearance associated with their early appearance ✓
  - ▶ Escape mutations have been observed experimentally X

## Key open question:

How “broadly-neutralizing” are the identified HmAbs?

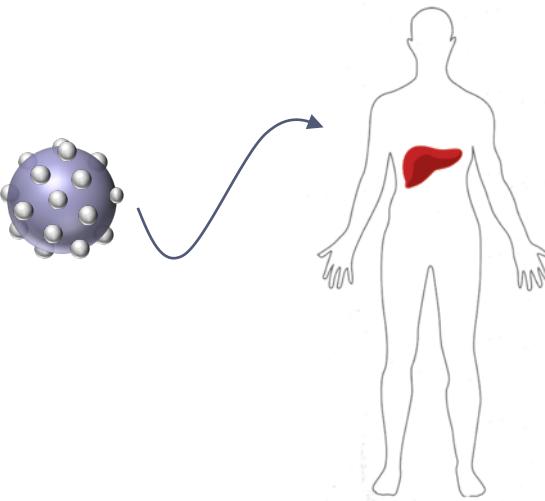
Which ones are the most difficult to escape?



## Proposed strategy:

Use sequence data of E2, statistical modeling and inference to try to identify escape-resistant HmAbs that can aid HCV vaccine development

# Within-host viral evolution model



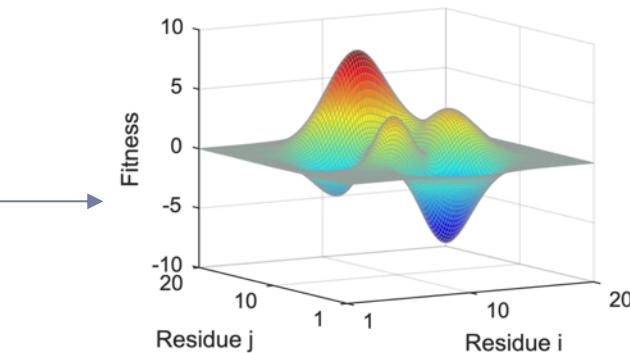
## Mutation

## Selection

High fitness  
Low fitness

## **Fitness landscape required**

## Experimental approach

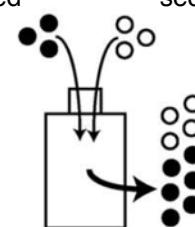


## E2 protein sequences

## Fitness of each sequence

Sequence to  
be measured

## Reference sequence



## Alternative Solution:

## Data-driven computational approach

# E2 fitness landscape inference – Unsupervised ML approach

## Available E2 data

**3,363** sequences of  
**363** residues long E2 protein extracted  
from **1,298** HCV-infected individuals  
**(subtype 1a)**

**Statistical model:  
Maximum entropy (prevalence) model**

$$f(\mathbf{x}) \sim p(\mathbf{x}) = \frac{\exp[-E(\mathbf{x})]}{Z}$$

## Maximum entropy formulation

$$\max S = - \sum_{\mathbf{x}} p(\mathbf{x}) \log p(\mathbf{x})$$

$$\text{s.t. } \sum_{\mathbf{x}} p(\mathbf{x}) = 1$$

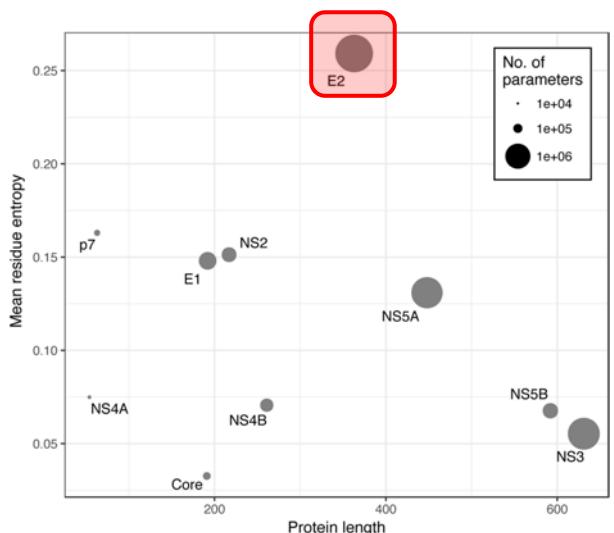
$$\sum_{\mathbf{x}} p(\mathbf{x}) \delta(x_i, a) = p_i^{obs}(a)$$

$$\sum_{\mathbf{x}} p(\mathbf{x}) \delta(x_i, a) \delta(x_i, b) = p_{ij}^{obs}(a | b)$$

## Solution:

$$(\mathbf{h}^*, \mathbf{J}^*) = \arg \min_{\mathbf{h}, \mathbf{J}} \text{KL}(p_0 || p_{\mathbf{h}, \mathbf{J}})$$

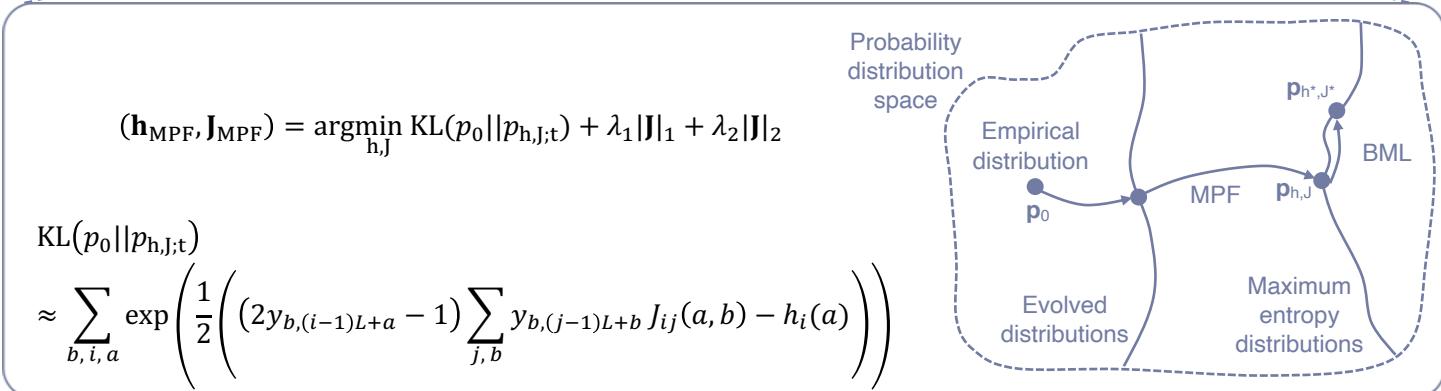
**Challenge:**  
Huge number of parameters



Framework for model inference

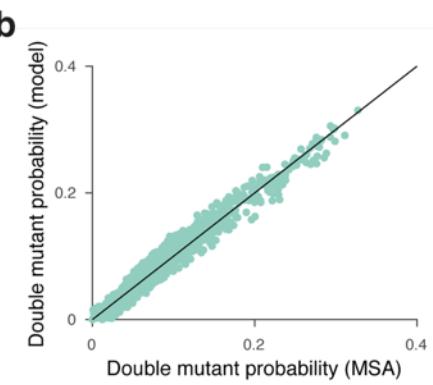
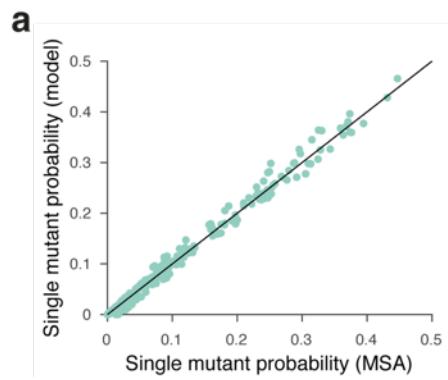
$$(\mathbf{h}_{\text{MPF}}, \mathbf{J}_{\text{MPF}}) = \operatorname{argmin}_{\mathbf{h}, \mathbf{J}} \text{KL}(p_0 || p_{\mathbf{h}, \mathbf{J}; t}) + \lambda_1 \|\mathbf{J}\|_1 + \lambda_2 \|\mathbf{J}\|_2$$

$$\begin{aligned} & \text{KL}(p_0 || p_{\mathbf{h}, \mathbf{j}; \mathbf{t}}) \\ & \approx \sum_{b, i, a} \exp \left( \frac{1}{2} \left( (2y_{b, (i-1)L+a} - 1) \sum_{j, b} y_{b, (j-1)L+b} J_{ij}(a, b) - h_i(a) \right) \right) \end{aligned}$$



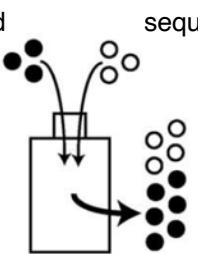
# E2 fitness landscape validation

## Statistical validation

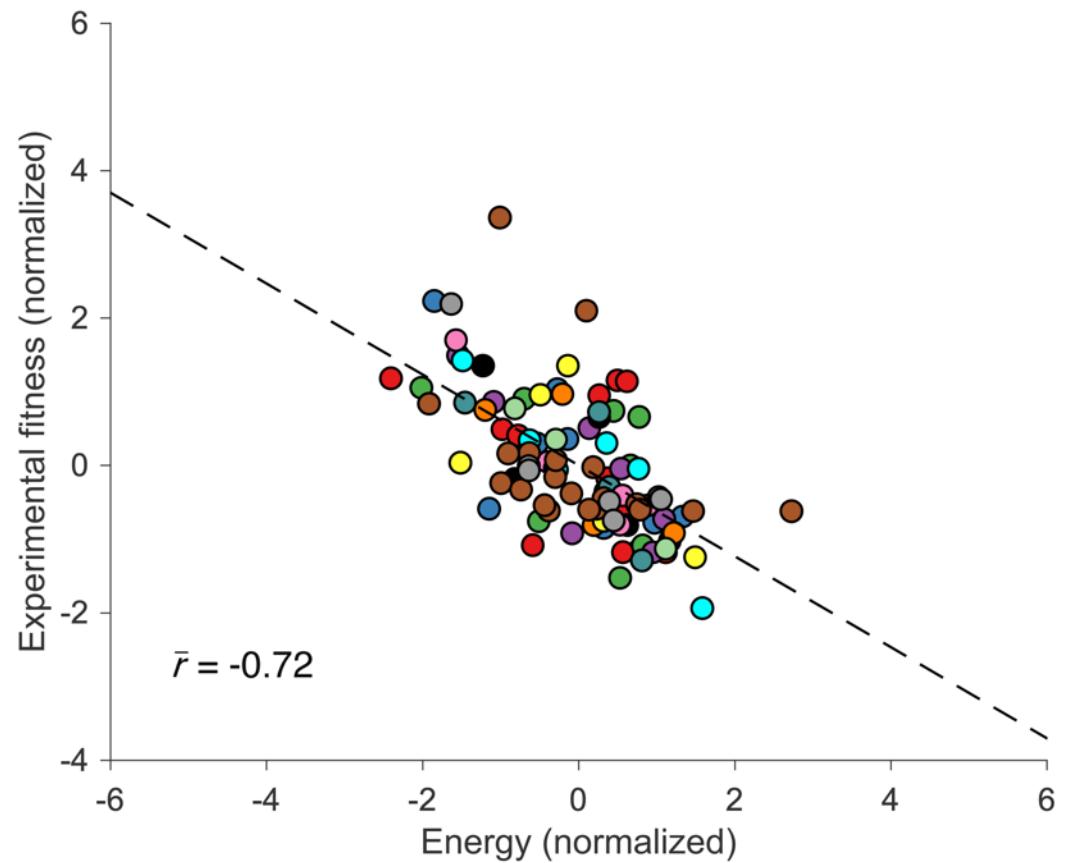


Sequence to  
be measured

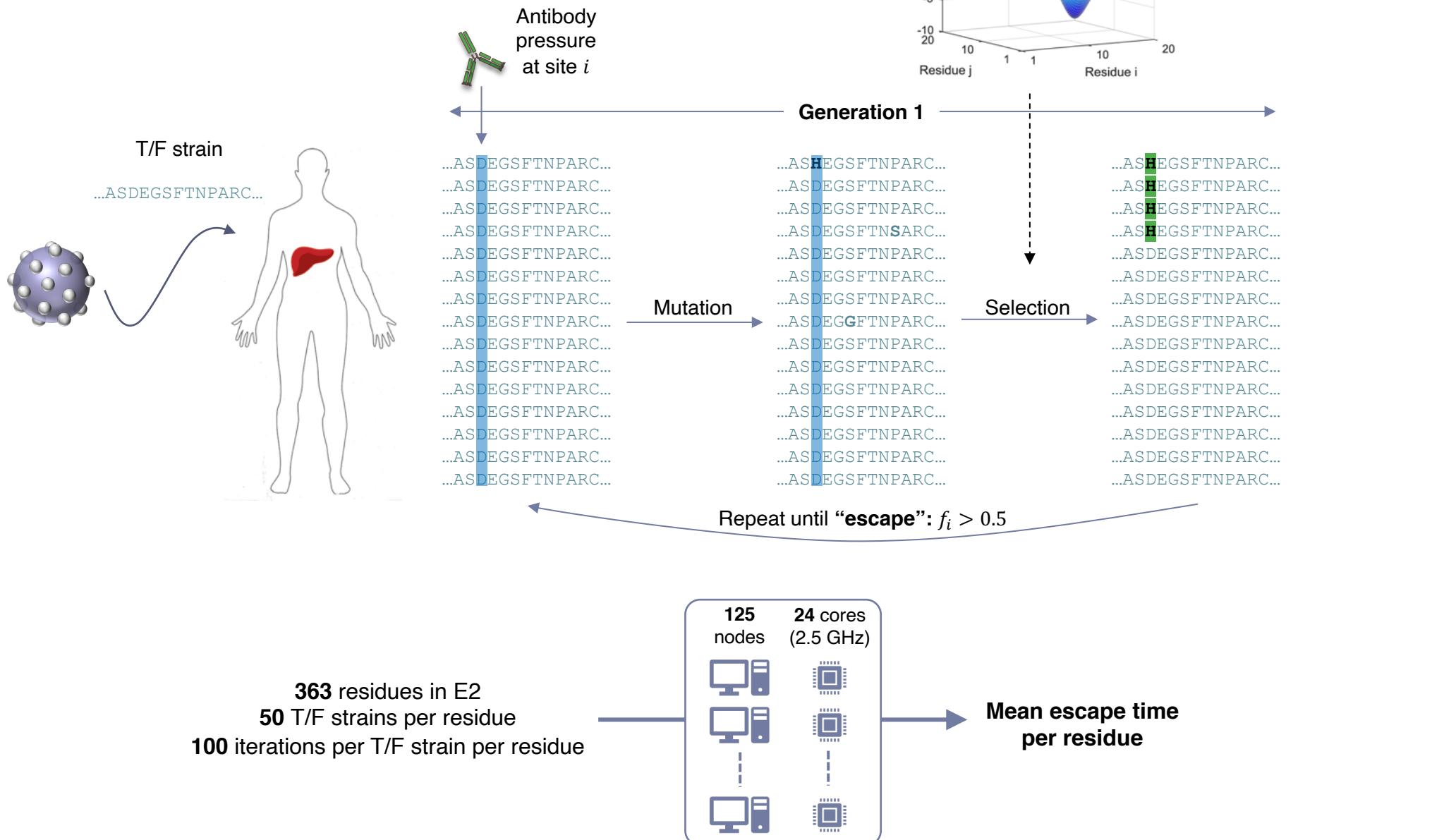
Reference  
sequence



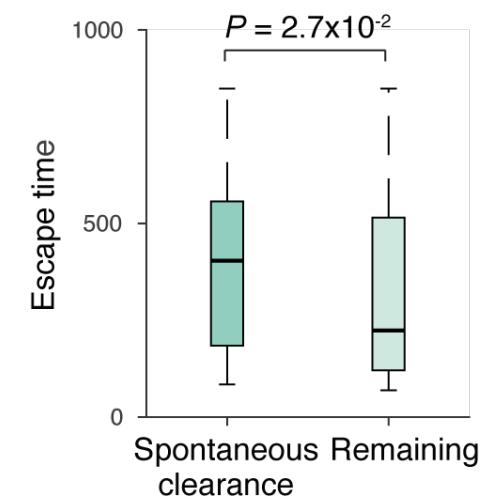
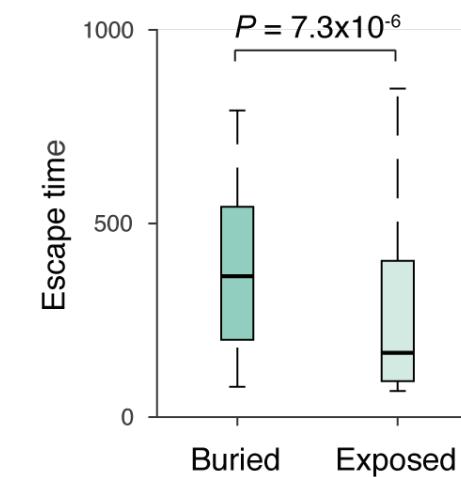
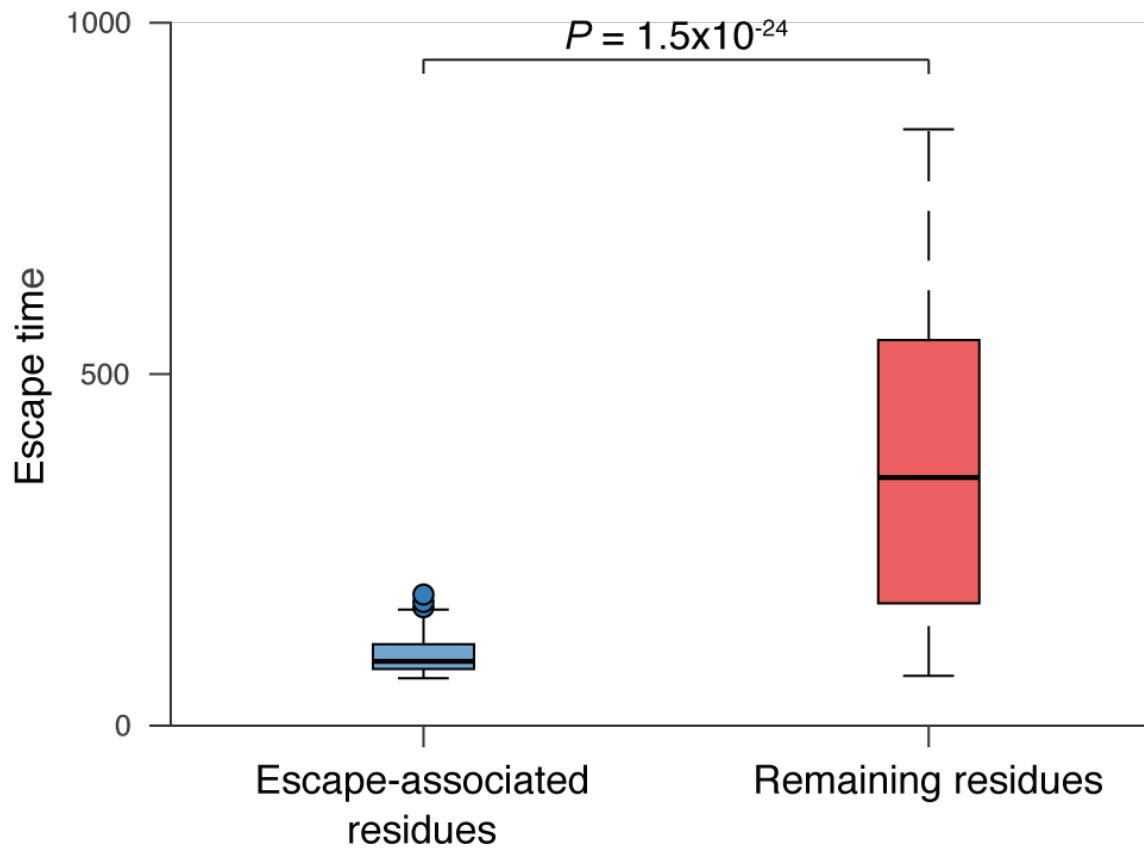
## Biological validation



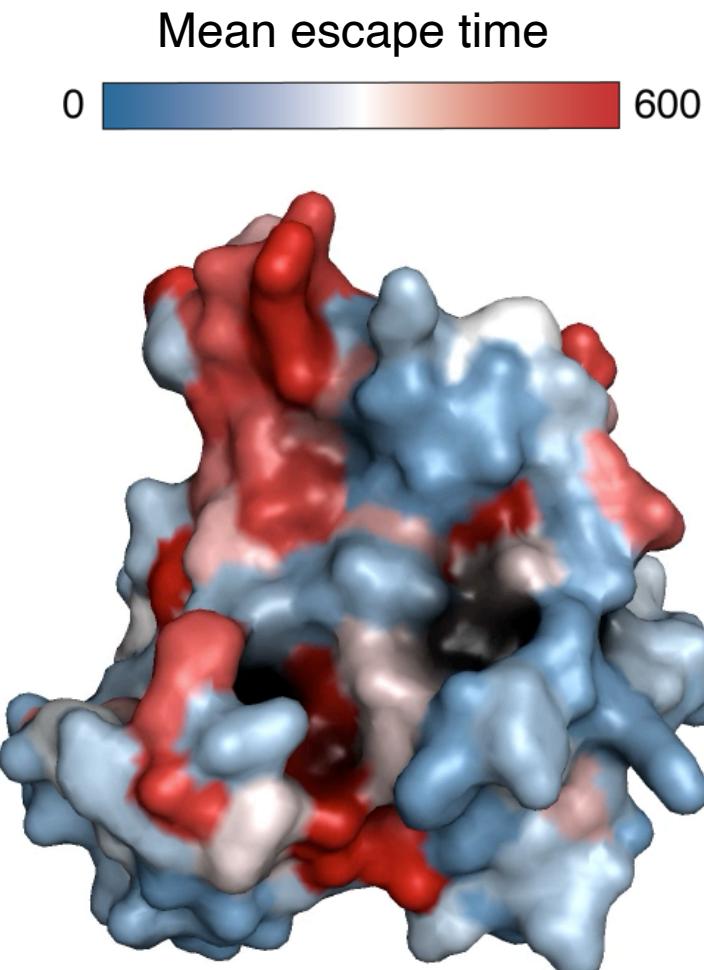
# Within-host viral evolution model



# Validation against experimental/clinical data

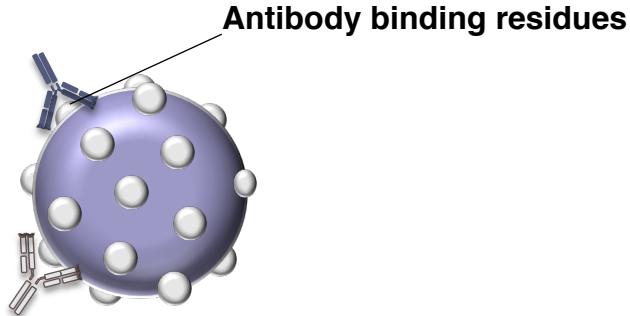


# Mapping the predicted escape times on HCV E2 structure

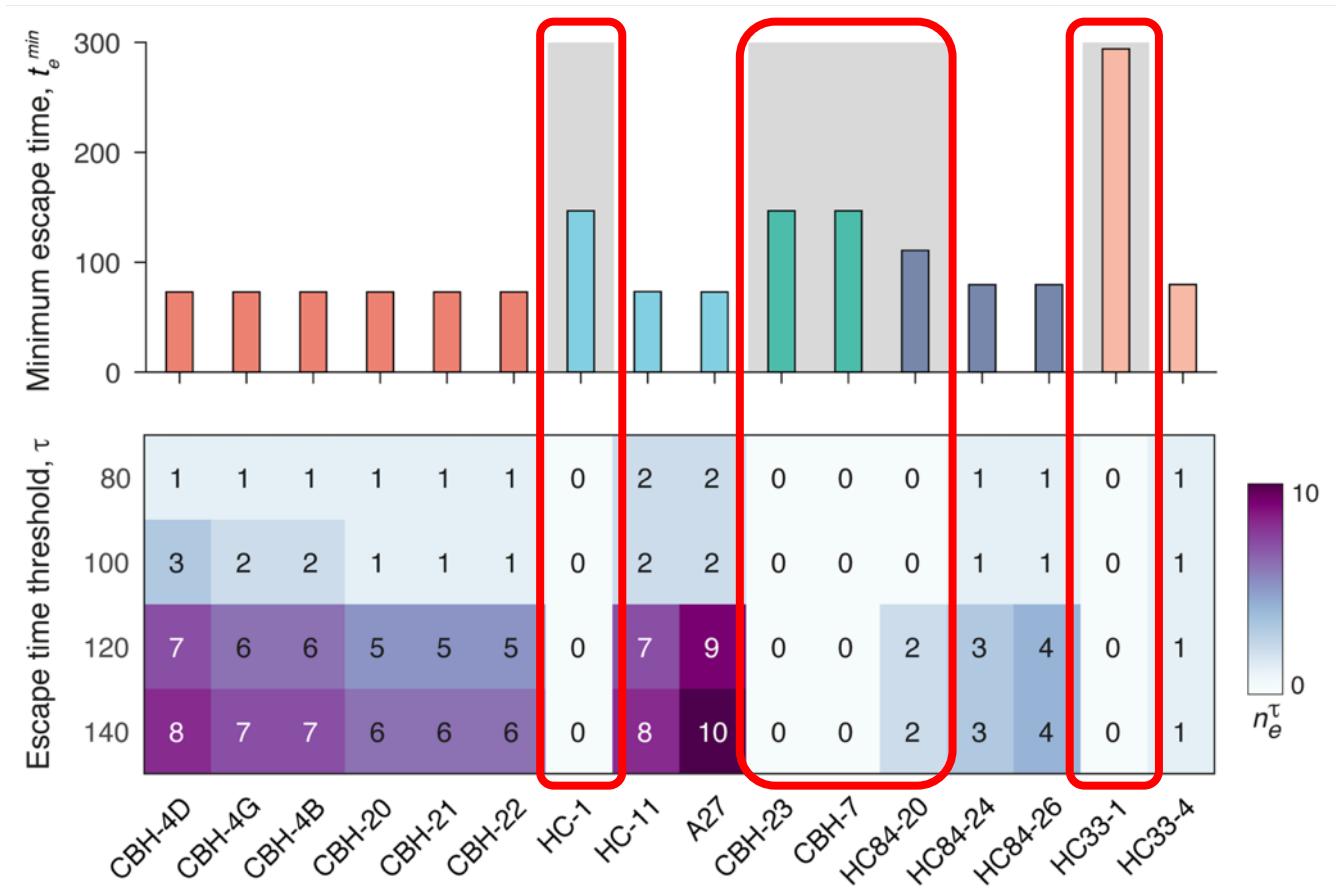
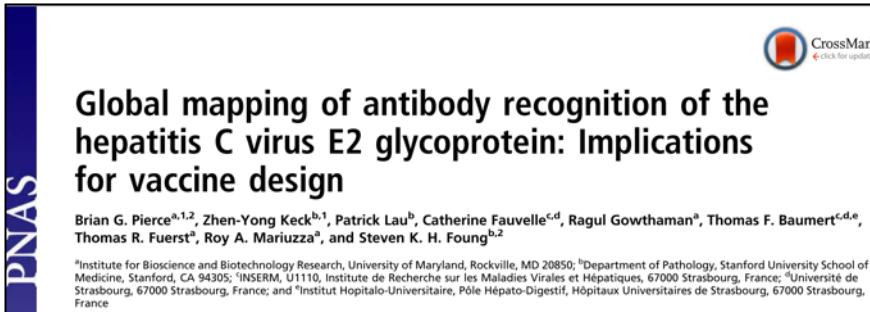


Protein data bank, <https://www.rcsb.org/> (PDB ID: 4MWF)

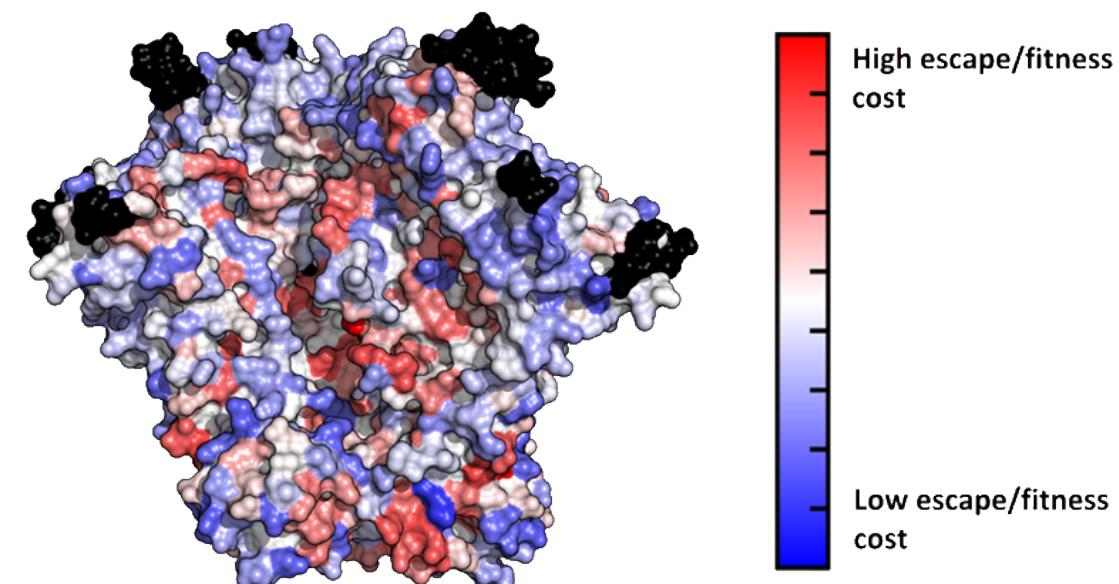
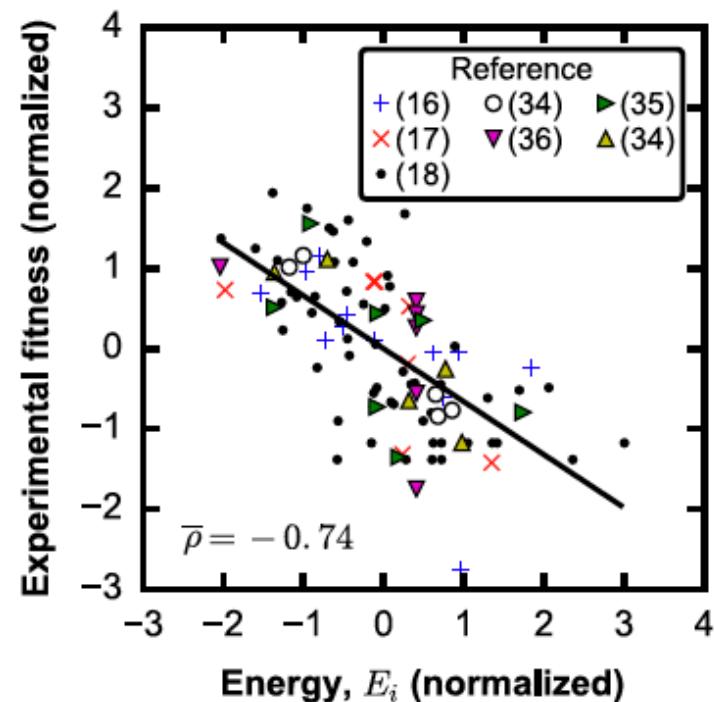
# Escape resistance of HmAbs



Antibody binding residues obtained from the recent extensive study by Pierce et al., 2016



# HIV gp160 (envelope) fitness landscape



# Part 1: Summary

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ARTICLE

<https://doi.org/10.1038/s41467-019-09819-1> OPEN

## Identifying immunologically-vulnerable regions of the HCV E2 glycoprotein and broadly neutralizing antibodies that target them

Ahmed A. Quadeer  <sup>1</sup>, Raymond H.Y. Louie  <sup>1,2,3,4</sup> & Matthew R. McKay  <sup>1,5</sup>



Ahmed



Ray (UNSW)

# PART 2: Finding vaccine targets for COVID-19

# SARS-CoV-2 and vaccine design

- ▶ Comparison of recent coronavirus infections in humans
  - ▶ SARS-CoV (2003 – 2004)<sup>1</sup>  
Infections: 8,098; Deaths: 774; Case-fatality rate: 15%
  - ▶ MERS-CoV (2012 – )<sup>2</sup>  
Infections: 2,494; Deaths: 858; Case-fatality rate: 34.4%
  - ▶ SARS-CoV-2 (2019 – )<sup>3</sup>  
Infections<sup>4</sup> : >7,000,000; Deaths : >400,000; Case-fatality rate<sup>5</sup> : 1.4%
- ▶ Clear need for an effective vaccine
- ▶ Our goal: help guide vaccine design by presenting early vaccine target recommendations
- ▶ Seek to *identify which parts of the virus may elicit a protective immune response?*
- ▶ Challenged by a lack of knowledge of SARS-CoV-2

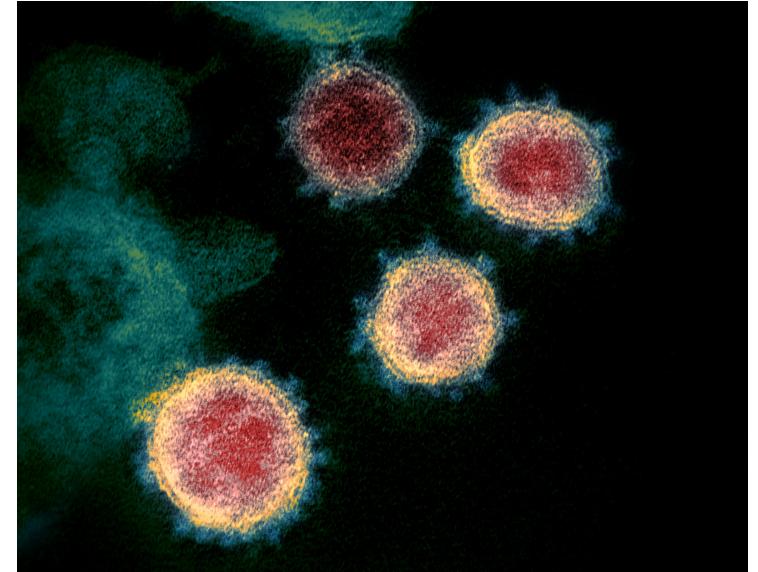
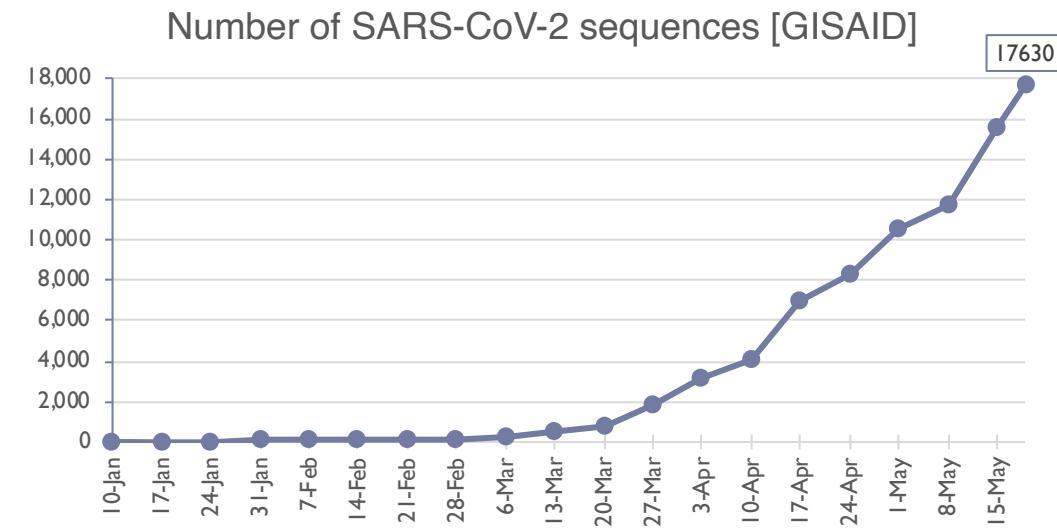
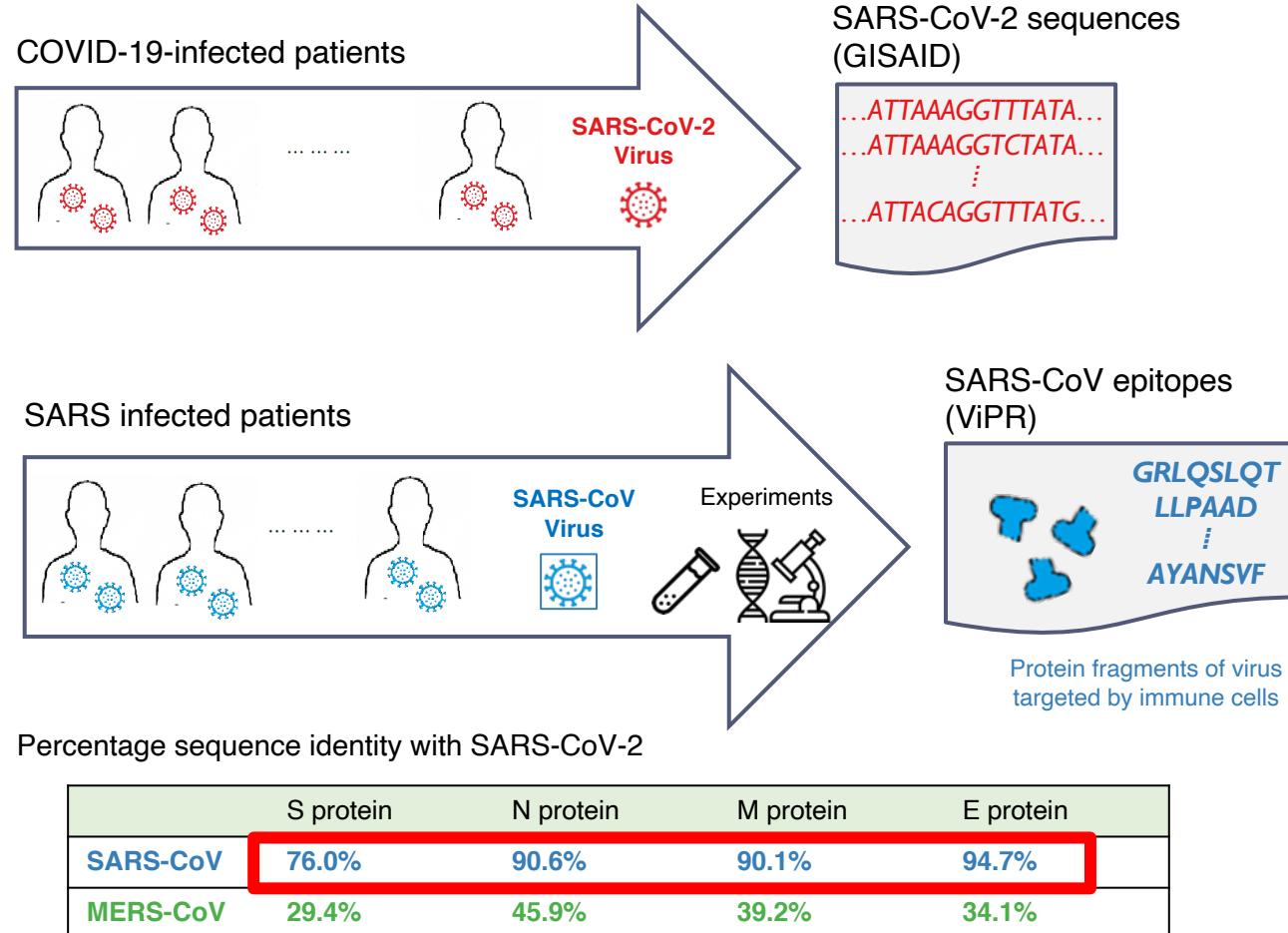


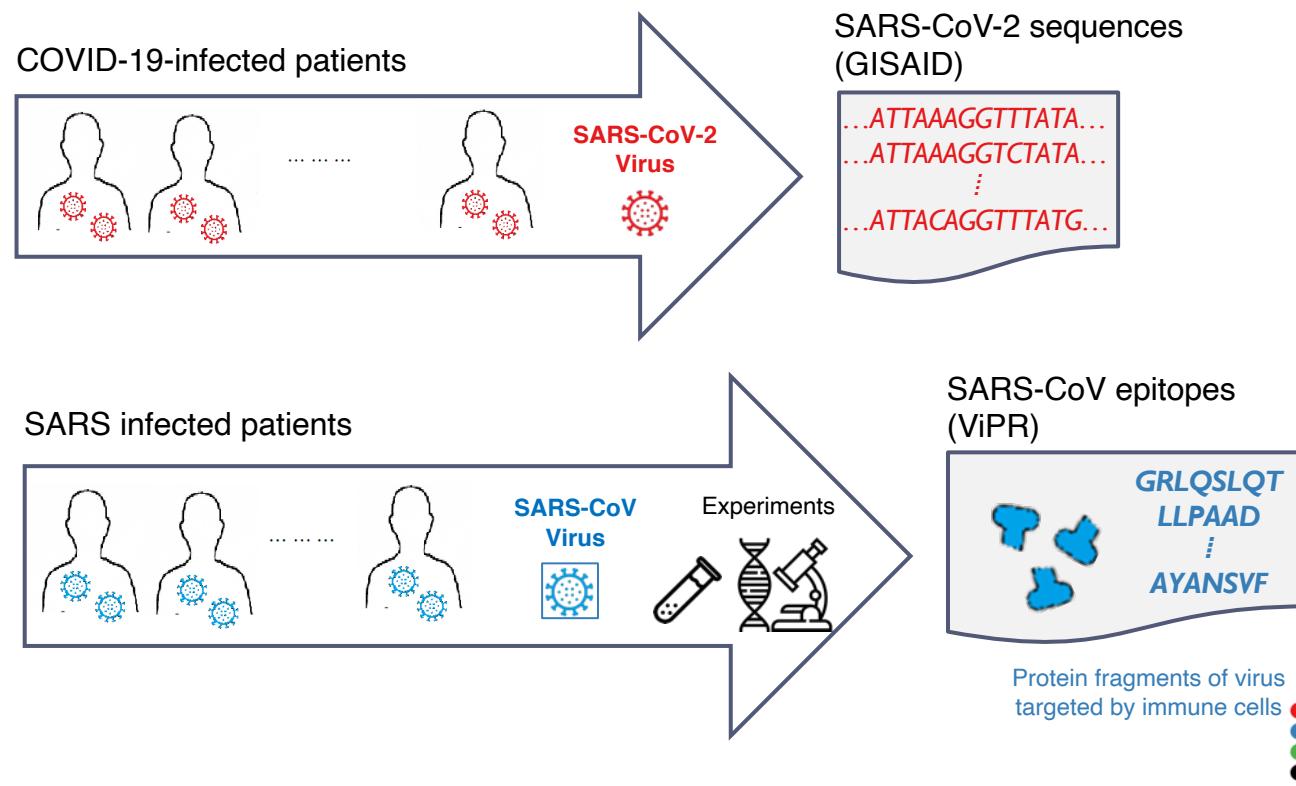
Image credit: NIH US

1. [https://www.who.int/csr/sars/archive/2003\\_05\\_07a/en/](https://www.who.int/csr/sars/archive/2003_05_07a/en/)  
2. <https://www.who.int/emergencies/mers-cov/en/>  
3. [https://www.who.int/docs/default-source/coronavirus/articles/coronavirus-\(covid-19\)-selected-bibliographic-references-18-02-2020-v1.pdf?sfvrsn=c8b8baa5\\_0](https://www.who.int/docs/default-source/coronavirus/articles/coronavirus-(covid-19)-selected-bibliographic-references-18-02-2020-v1.pdf?sfvrsn=c8b8baa5_0)  
4. <https://www.arcgis.com/apps/opsdashboard/index.html#/bda7594740fd40299423467b48e9ecf6>  
5. <https://www.med.hku.hk/en/covid-19/articles/fatality-rate-of-covid-19>

# Providing SARS-CoV-2 vaccine target recommendations



# Providing SARS-CoV-2 vaccine target recommendations



## Idea

Exploit **immunological data for SARS-CoV**  
to provide  
vaccine target recommendations for SARS-CoV-2

## Approach

Search for SARS-CoV epitopes  
with a **close genetic match**  
in SARS-CoV-2 sequences

## Output

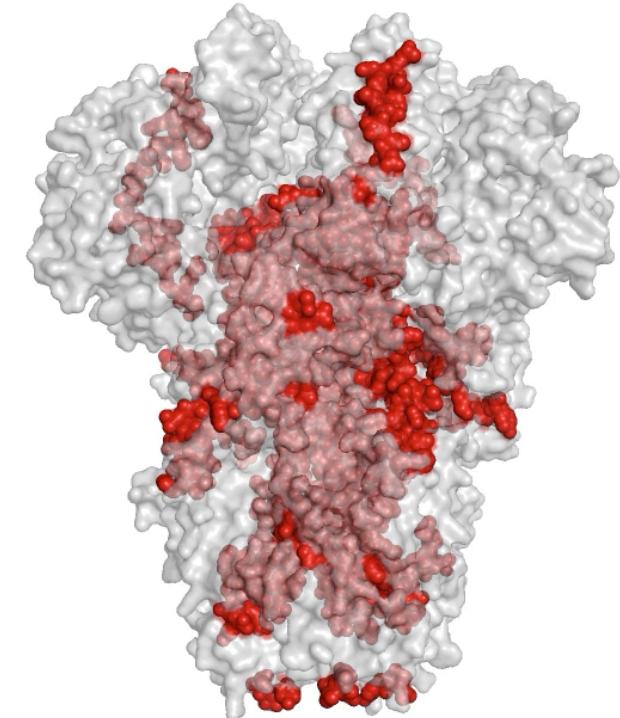
Potentially **immunogenic** epitopes

# Results summary

SARS-CoV epitopes	Percentage with identical genetic match in SARS-CoV-2
T cell epitopes	<b>24%</b>
B cell epitopes	<b>16%</b>
overall	<b>20%</b>

Identified set of T cell epitopes may provide broad population coverage globally (96%) as well as in China (88%)

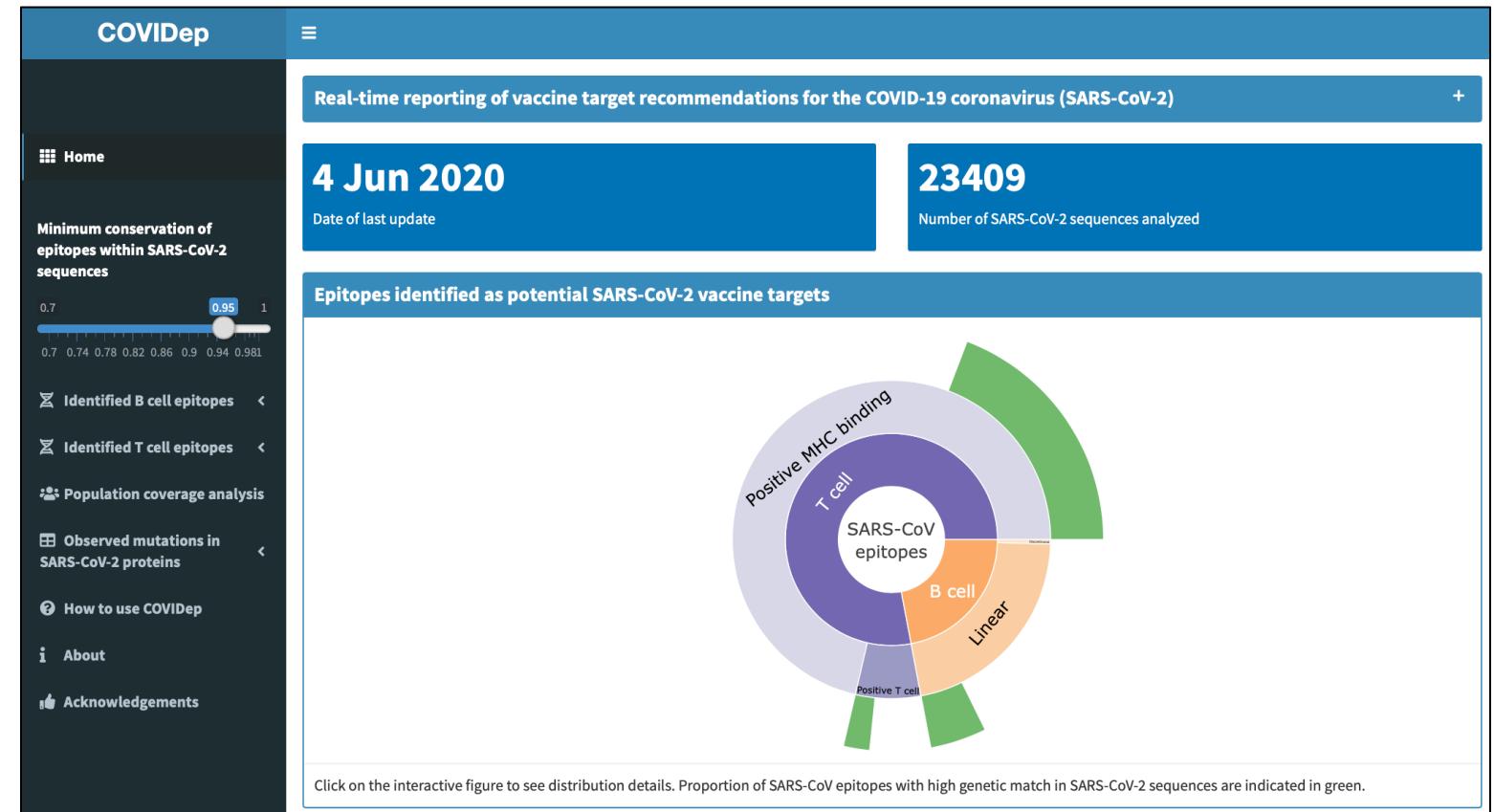
**B cell epitopes with an identical genetic match in SARS-CoV-2**



SARS-CoV spike protein  
(PDB ID: 5XLR)

# Extension: COVIDep <https://covidep.ust.hk>

- ▶ Increase in number of SARS-CoV-2 sequences
  - ▶ **120 → now over 25,000**
- ▶ COVIDep: A web-based platform for real-time reporting of vaccine target recommendations for SARS-CoV-2
- ▶ Features:
  - ▶ Identification of SARS-derived B-cell and T-cell epitopes that provide vaccine target recommendations for SARS-CoV-2;
  - ▶ For T cell epitopes, it reports estimated population coverage using HLA/MHC statistical information;
  - ▶ Up-to-date reporting based on latest sequence data available (from GISAID).



# Connections with COVID-19 B cell responses and preclinical vaccine trials

- ▶ Most (24/29) identified B cell epitopes of the spike protein are in the **S2 subunit**, reported to be a main region targeted by **cross-neutralizing antibodies**
  - ▶ Overlap with regions in the S1 subunit reported to be targeted by **cross-neutralizing antibodies**
  - ▶ Overlap with an epitope targeted by neutralizing antibodies in a **preclinical trial of a SARS-CoV-2 vaccine candidate**
  - ▶ Overlap with regions recognized by neutralizing antibodies in **recovered COVID-19 patients**

# Article

## Structure, Function, and Antigenicity of the SARS-CoV-2 Spike Glycoprotein



**nature**  
COMMUNICATIONS

ARTICLE

<https://doi.org/10.1038/s41467-020-16256-y> OPEN

 Check for updates

A human monoclonal antibody blocking SARS-CoV-2 infection

**nature** | SARS-CoV-2 INFECTION  
https://doi.org/10.1038/s41586-020-2349-y  
van Haperen<sup>2,3</sup>,  
eld &  
**Accelerated Article Preview**  
**Cross-neutralization of SARS-CoV-2 by a human monoclonal SARS-CoV antibody**

## A single dose SARS-CoV-2 simulating particle vaccine induces potent neutralizing activities

Di Yin<sup>1,2</sup>, Sikai Ling<sup>1,2</sup>, Xiaolong Tian<sup>2,3</sup>, Yang Li<sup>1</sup>, Zhijie Xu<sup>1</sup>, Hewei Jiang<sup>1</sup>, Xue Zhang<sup>1</sup>, Xiaoyuan Wang<sup>3</sup>, Yi Shi<sup>4</sup>, Yan Zhang<sup>1</sup>, Lintai Da<sup>1</sup>, Sheng-ce Tao<sup>1</sup>, Quanjun Wang<sup>5</sup>, Jianjiang Xu<sup>6</sup>, Tianlei Ying<sup>2,3\*</sup>, Jiaxu Hong<sup>6,7,\*</sup> and Yujia Cai<sup>1,\*</sup>

**nature**  
COMMUNICATIONS

Details of the identified B cell epitopes in the S protein											
Show	50	entries	Download csv	Search:							
IEDB	↑↓	Epitope	↑↓	Length	↑↓	Start	↑↓	End	↑↓	Conservation	↑↓
30987		KGIYQTSN		8		310		317		0.9646	
70719		<u>VRFPNITNLCPFGEVN</u>		17		327		343		0.9948	
15972		<u>FGEVFNAT</u>		8		338		345		0.9976	
52020		<u>QQFGRD</u>		6		563		568		0.9999	
18594		GAGICASY		8		667		674		0.9993	
22321		GSFCTQLN		8		757		764		0.9996	
16183		<u>FIEDLLFNKVTLADAGF</u>		17		817		833		0.9952	
18515		GAALQIPFAMQMAYRFN		17		891		907		0.9989	
47479		PFAMQMAYRFNGIGVTQ		17		897		913		0.9993	
3176		AMQMAYRF		8		899		906		0.9994	
41177		MAYRFNGIGVTQNVLYE		17		902		918		0.9995	
10778		DVVNQNAQALNTLVKQL		17		950		966		0.9988	
50311		QALNTLVKQLSSNFGAI		17		957		973		0.999	
2092		AISSVLNDILSRLDKVE		17		972		988		0.9994	
27357		ILSLRDKVEAEVQIDRL		17		980		996		0.9997	
11038		EAEVQIDRLITGRLQLS		17		988		1004		0.9997	
54599		RLITGRLQLSQTYVTQQ		17		995		1011		0.9997	
59425		SLQTYVTQQLIRAAEIR		17		1003		1019		0.9995	
51379		QLIRAAEIRASANLAAT		17		1011		1027		0.9979	
53202		RASANLAATKMSECVLG		17		1019		1035		0.998	
462		AATKMSECVLGQSKRVD		17		1025		1041		0.9989	
67220		TVYDPLQPELDSKEEL		17		1136		1152		0.9696	
32508		KNHTSPDVLDGDISGIN		17		1157		1173		0.9974	
9094		<u>DLGDISGINASVNVNIQK</u>		17		1165		1181		0.9981	
12426		<u>EIDRLNEVAKNLNESLIDLQELGKYEQY</u>		28		1182		1209		0.9974	
558417		<u>EIDRLNEVAKNLNESLIDLQELGKYEQY</u>		28		1182		1209		0.9974	
14626		EVAKNLNESLIDLQELG		17		1188		1204		0.9979	
6476		CKFDEDSDSEPVLGVKLHYT		20		1254		1273		0.9911	
7868		DDSEPVLGVKLHYT		15		1259		1273		0.9914	

# Connections with COVID-19 T cell responses and preclinical vaccine trials

- Of the 14 HLA-A\*02:01-restricted spike protein epitopes identified by COVIDep, **9 epitopes** overlap with SARS-CoV-2 **immunogenic epitopes**.

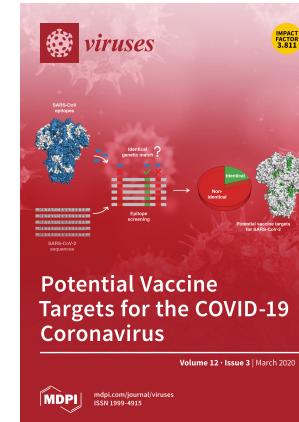
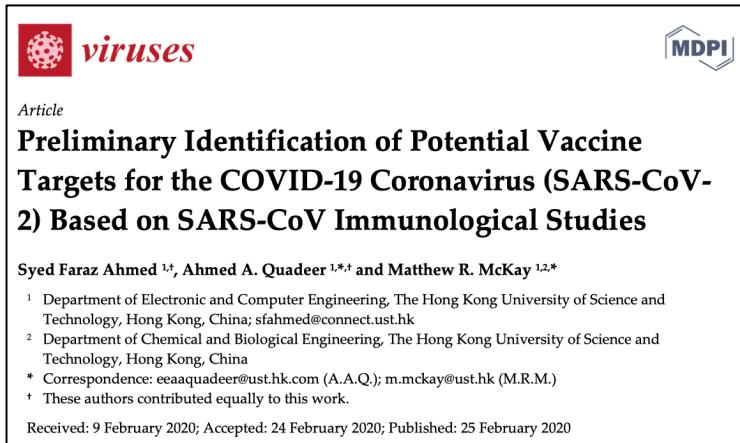
Shared Antigen-specific CD8 <sup>+</sup> T cell Responses Against the SARS-CoV-2 Spike Protein in HLA-A*02:01 COVID-19 Participants	
William Chour <sup>1,2,3</sup> , Alexander M. Xu <sup>1,4</sup> , Alphonsus H.C. Ng <sup>1,4</sup> , Jongchan Choi <sup>1</sup> , Jingyi Xie <sup>1,5</sup> , Dan Yuan <sup>1,6</sup> , Diana C. DeLucia <sup>7</sup> , Rick A. Edmark <sup>1</sup> , Lesley C. Jones <sup>1</sup> , Thomas M. Schmitt <sup>8</sup> , Mary E. Chaffee <sup>8</sup> , Venkata R. Duvvuri <sup>1</sup> , Kim M. Murray <sup>1</sup> , Songming Peng <sup>9</sup> , Julie Wallick <sup>10</sup> , Heather A. Algren <sup>10</sup> , William R. Berrington <sup>10</sup> , D. Shane O'Mahony <sup>10</sup> , John K. Lee <sup>7,11</sup> , Philip D. Greenberg <sup>8,12</sup> , Jason D. Goldman <sup>10,13*</sup> , and James R. Heath <sup>1*</sup>	
SARS-CoV-2 epitopes are recognized by a public and diverse repertoire of human T-cell receptors	
Alina S. Shomuradova <sup>1</sup> , Murad S. Vagida <sup>1</sup> , Savely A. Sheetikov <sup>1</sup> , Ksenia V. Zornikova <sup>1</sup> , Dmitriy Kiryukhin <sup>1</sup> , Aleksei Titov <sup>1</sup> , Iuliia O. Peshkova <sup>1</sup> , Alexandra Khmelevskaya <sup>1</sup> , Dmitry V. Dianov <sup>1</sup> , Maria Malashova <sup>1</sup> , Anton Shmelev <sup>1</sup> , Yana Serdyuk <sup>1</sup> , Dmitry V. Baqaev <sup>2</sup> , Anastasia Plynyuk <sup>3</sup> , Dmitri S. Scherbinin <sup>4,5</sup> , Alexandra V. Maleeva <sup>1</sup> , Naina T. Shakirova <sup>1</sup> , Artem Pilunov <sup>1</sup> , Dmitry B. Makov <sup>1</sup> , Ekaterina G. Khamaganova <sup>1</sup> , Bella Biderman <sup>1</sup> , Alexander Ivanov <sup>6</sup> , Mikhail Shugay <sup>3,4,5</sup> and Grigory A. Efimov <sup>1</sup>	

- In a **preclinical vaccine trial**, T cell responses have also been recorded against a protein region comprising a COVIDep-identified epitope



Details of the identified T cell epitopes in the S protein						
Show	25	entries	Download csv	Search:	HLA-A*02:01	Conservation
IEDB	Epitope	Length	Start	End	MHC allele class	
36724	<u>LITGRLQSL</u>	9	996	1004	I	HLA-A2/HLA-A*02:01 0.9998
54507	<u>RLDKVEAEV</u>	9	983	991	I	HLA-A*02:01/HLA-A*02:02/HLA-A*02:06/HLA-A*02:03/HLA-A*68:02 0.9998
54725	<u>RLQLSQLTYV</u>	9	1000	1008	I	HLA-A*02:01/HLA-A*02:02/HLA-A*02:03/HLA-A*02:06/HLA-A*68:02 0.9998
37544	<u>LLLQYGSFC</u>	9	752	760	I	HLA-A*02:01 0.9997
37724	<u>LLQYGSFCT</u>	9	753	761	I	HLA-A*02:01 0.9997
69657	<u>VLNLDLSRL</u>	9	976	984	I	HLA-A*02:01 0.9997
71663	<u>VVFLHVTVW</u>	9	1060	1068	I	HLA-A*02:01/HLA-A*02:02/HLA-A*02:03/HLA-A*02:06/HLA-A*68:02 0.9995
2801	<u>ALNTLVKQL</u>	9	958	966	I	HLA-A*02:01 0.9994
44814	<u>NLNESLIDL</u>	9	1192	1200	I	HLA-A*02:01 0.9993
26710	<u>IITTDNTFV</u>	9	1114	1122	I	HLA-A*02:01 0.9992
54680	<u>RLNEVAKNL</u>	9	1185	1193	I	HLA-A*02:01 0.9992
16156	<u>FIAGLIAIV</u>	9	1220	1228	I	HLA-A*02:01/HLA-A*02:02/HLA-A*02:03/HLA-A*02:06/HLA-A*68:02/HLA-A2 0.9991
20907	<u>GLIAIVMVTI</u>	10	1223	1232	I	HLA-A*02:02/HLA-A*02:03/HLA-A*02:01/HLA-A*02:06/HLA-A*68:02 0.9985
37289	<u>LLFNKVTLA</u>	9	821	829	I	HLA-A*02:01/HLA-A*02:02/HLA-A*02:03/HLA-A*02:06/HLA-A*68:02 0.9976
Showing 1 to 14 of 14 entries (filtered from 75 total entries)						
		Previous		1	Next	

# Part 2: Summary



**COVIDep platform for real-time reporting of vaccine target recommendations for SARS-CoV-2: Description and connections with COVID-19 immune responses and preclinical vaccine trials**

Syed Faraz Ahmed<sup>1</sup>, Ahmed A. Quadeer<sup>1,†</sup>, Matthew R. McKay<sup>1,2,†</sup>

<sup>1</sup>Department of Electronic and Computer Engineering, The Hong Kong University of Science and Technology, Hong Kong, China

<sup>2</sup>Department of Chemical and Biological Engineering, The Hong Kong University of Science and Technology, Hong Kong, China

†Joint corresponding authors: [eaaquadeer@ust.hk](mailto:eaaquadeer@ust.hk) and [m.mckay@ust.hk](mailto:m.mckay@ust.hk)



## Some informative reviews on COVID-19 vaccine development

1. T. T. Le, et al, The COVID-19 vaccine development landscape, *Nature Reviews Drug Discovery*, April 2020
2. F. Amanat, F. Krammer, "SARS-CoV-2 vaccines: Status report, *Immunity*, April 2020
3. E. Callaway, "The race for coronavirus vaccines", *Nature*, April 2020

# PART 3:

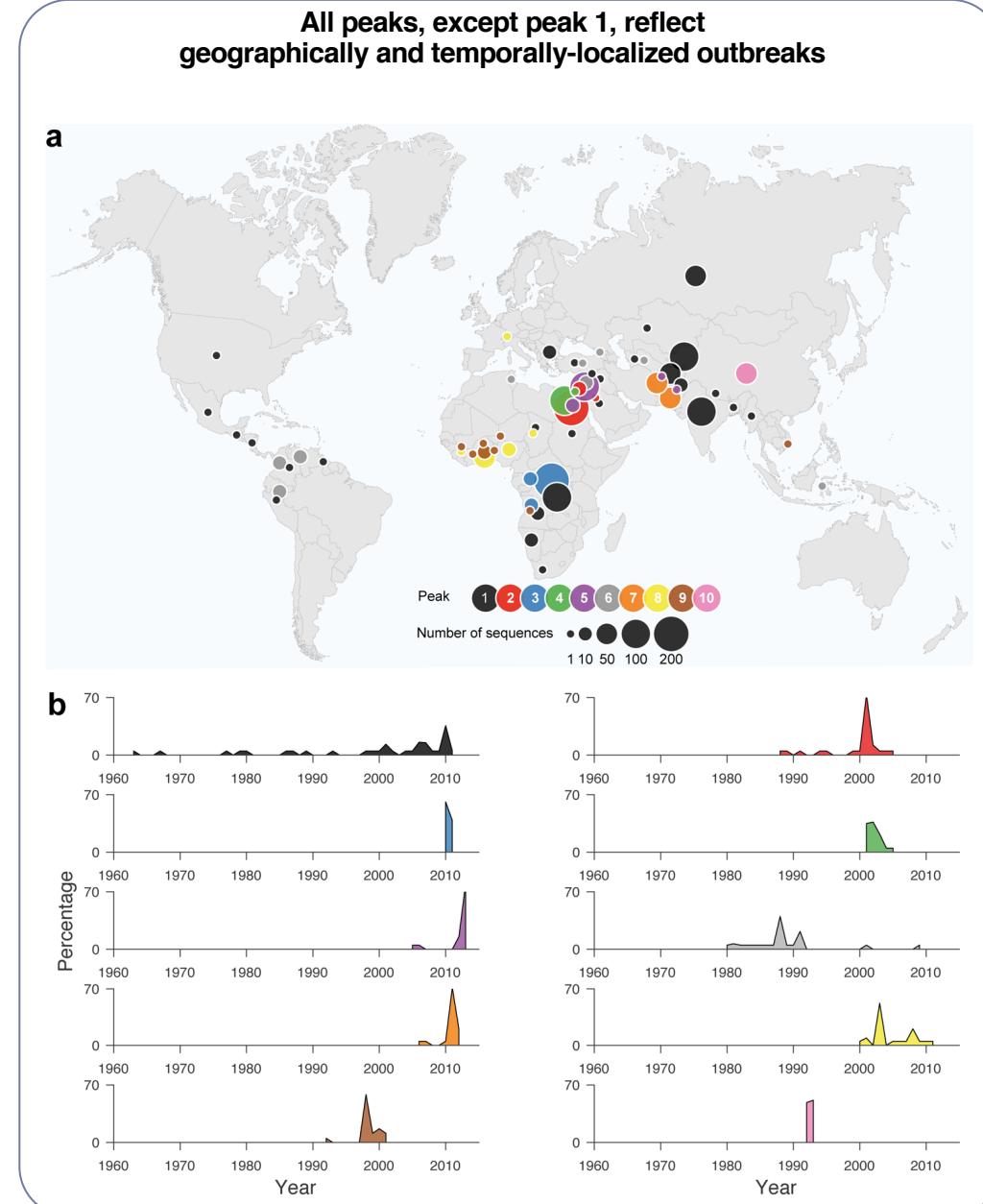
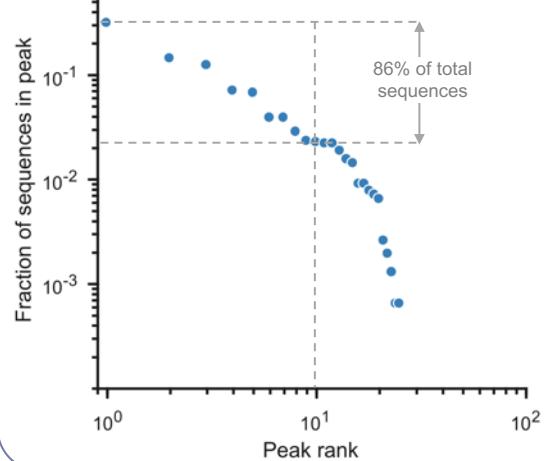
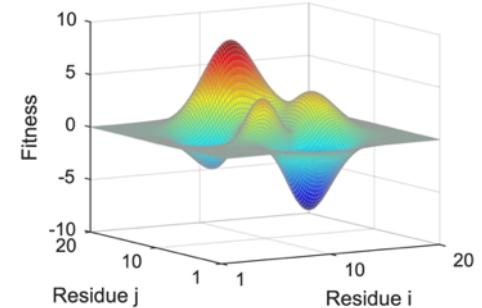
# Other related projects

# Using maximum entropy model to explore why the polio vaccine is so effective

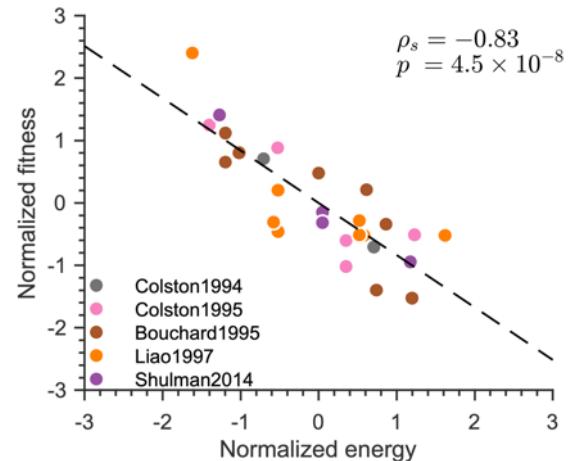
Fitness  $\times$  Prevalence

$$f(\mathbf{x}) \sim p(\mathbf{x}) = \frac{\exp[-E(\mathbf{x})]}{Z}$$

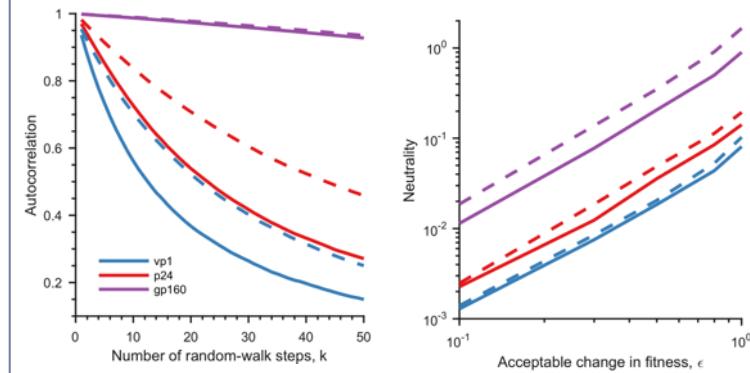
Inferred landscape comprises multiple peaks



Landscape based on peak 1 reflects intrinsic fitness landscape

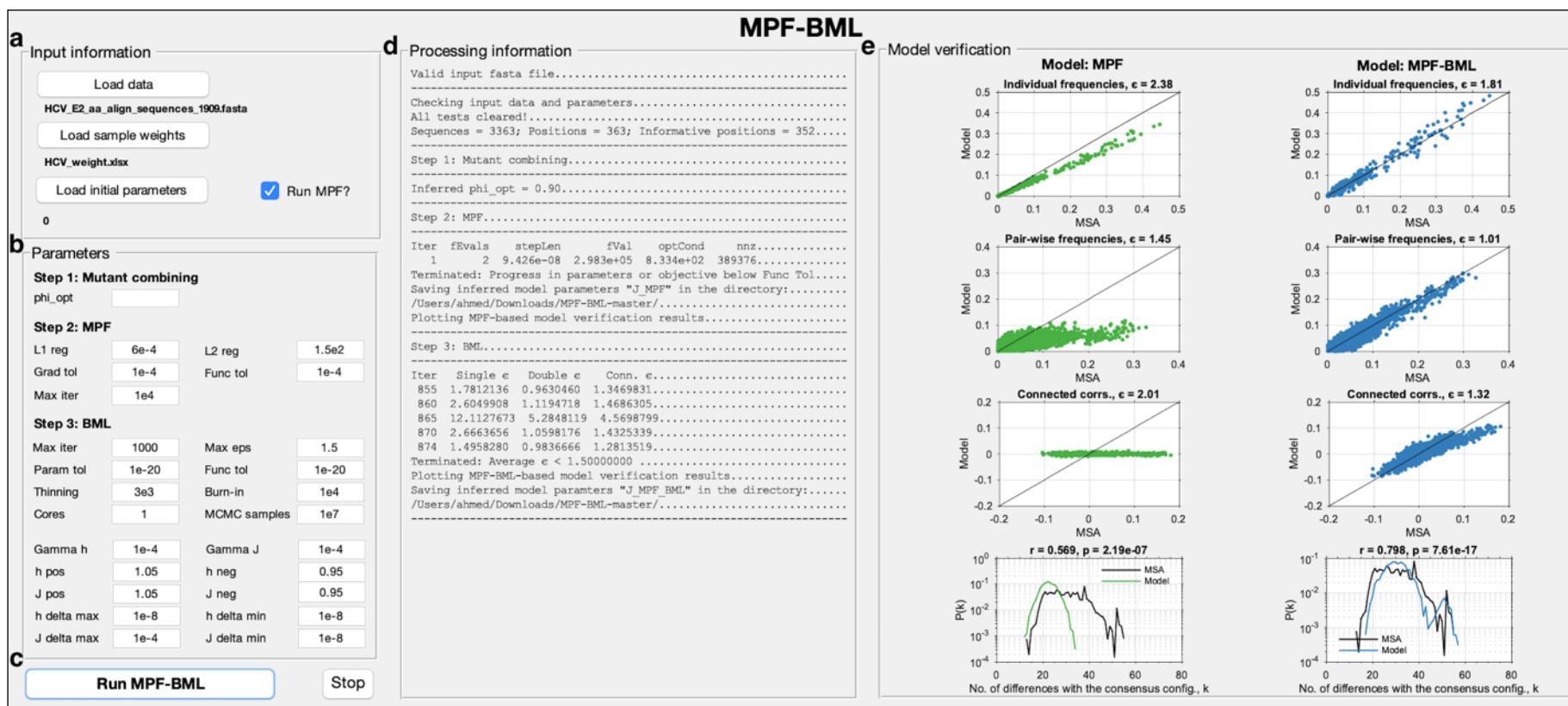


Compared to HIV proteins, PV is subject to more restrictive constraints



# MPF-BML: A standalone GUI-based package for maximum entropy model inference

- ▶ **Standalone**—no requirement of any pre-installed application;
- ▶ **Cross-platform**—works for Windows, Linux, and mac OS;
- ▶ **GUI-based**—no knowledge of any programming language required;
- ▶ **Minimum input requirement**—only sample data and sample weights (if available) required;
- ▶ **Publication-quality figures output**—all results are saved as vector graphics.

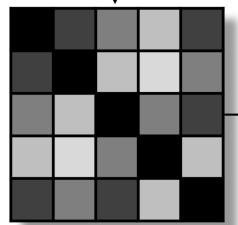
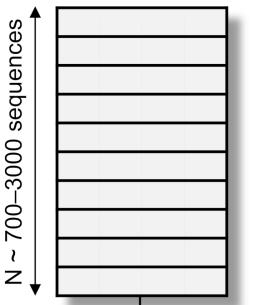


# Robust co-evolutionary analysis (RoCA) of proteins

A

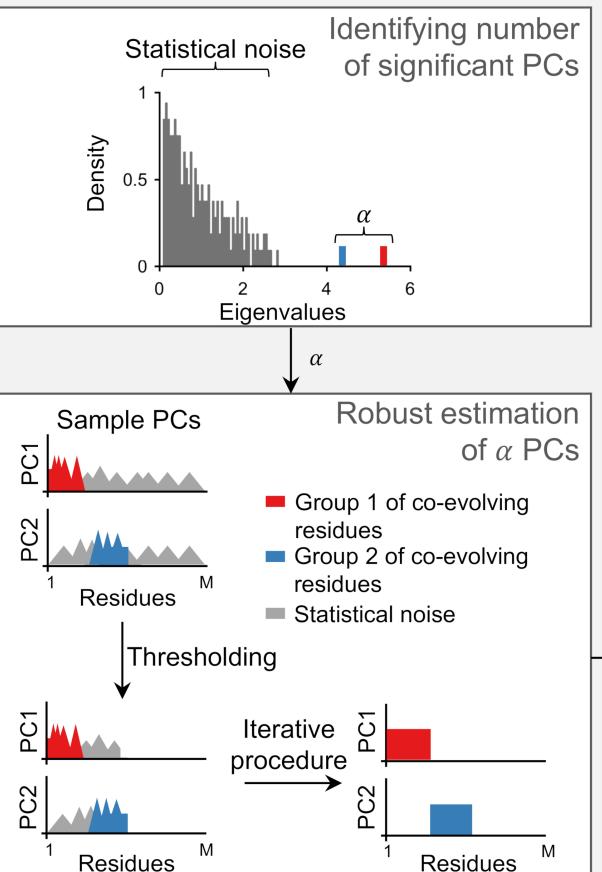
Multiple sequence alignment  
 $M \sim 200\text{--}700$  residues

$N \sim 700\text{--}3000$  sequences

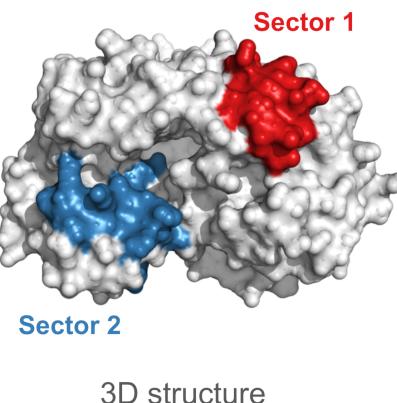


Pearson correlation matrix

B



C



## RMT-based sparse PCA (SPCA)

- ▶ Pioneer work – Diagonal thresholding [Johnstone 2009]
- ▶ Augmented SPCA [Paul 2012]
- ▶ **Iterative thresholding SPCA (ITSPCA) [Ma 2013]**

## Summary

- Based on “orthogonal iteration method”
- Estimates sparse subspace of the leading eigenvectors
- Steps involved:
  - Projecting the correlation matrix on a subspace
  - Thresholding the columns of the resultant matrix using a **thresholding** parameter
  - Repeat until convergence

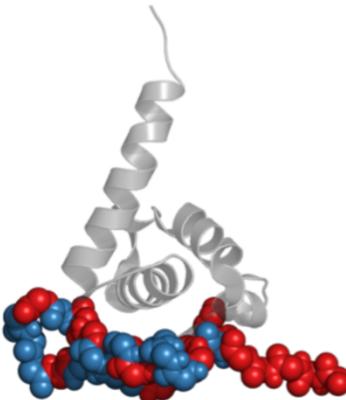


## Robust Co-evolutionary Analysis (RoCA)

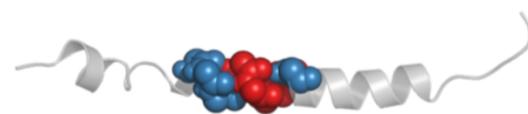
- Adapted to work on correlation matrices
- A data-driven **thresholding** parameter designed using ideas from random matrix theory

# HIV Gag

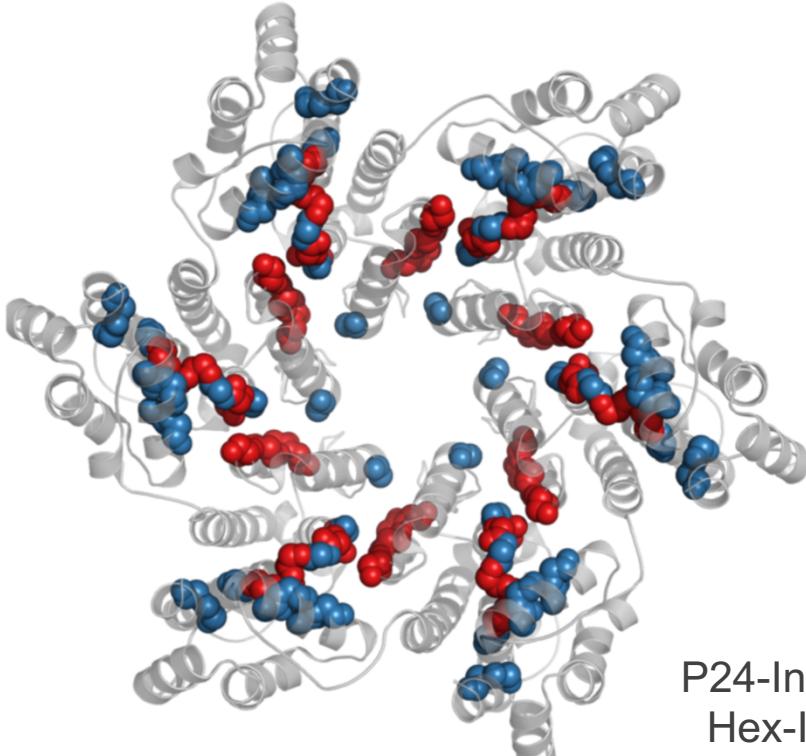
P17-Mem-Bin-Dom



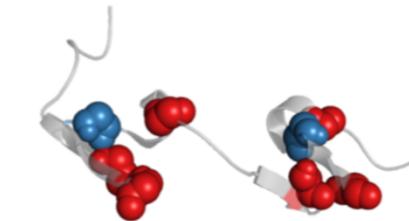
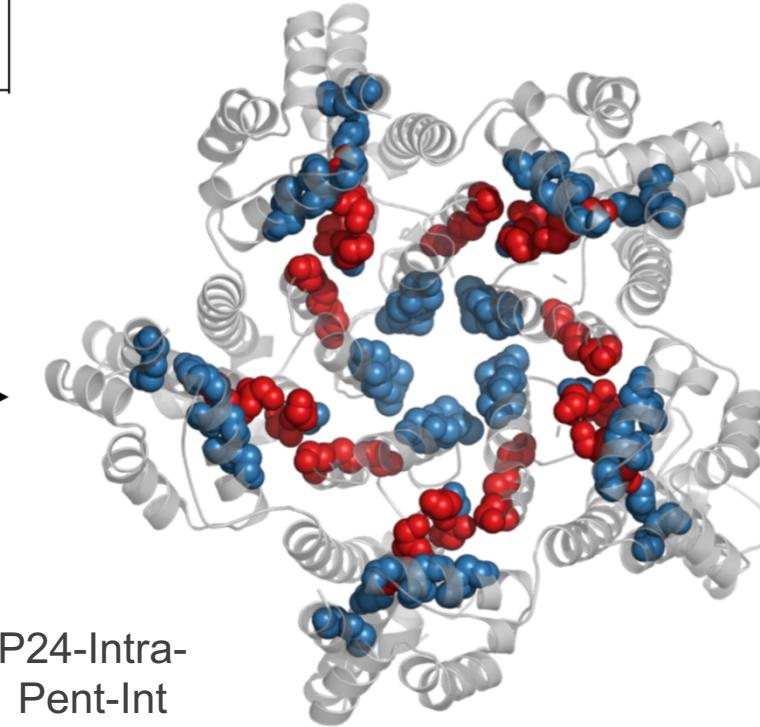
P24-SP1-Int



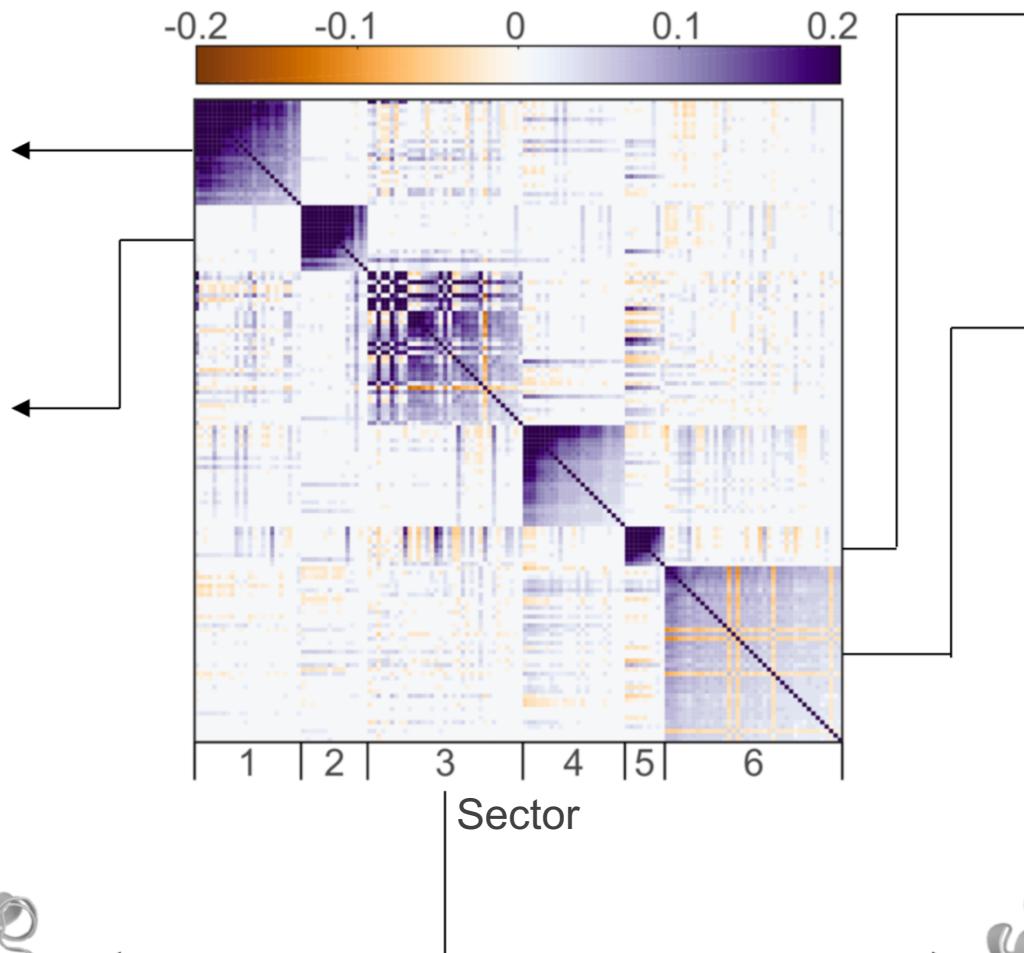
P24-Intra-Hex-Int



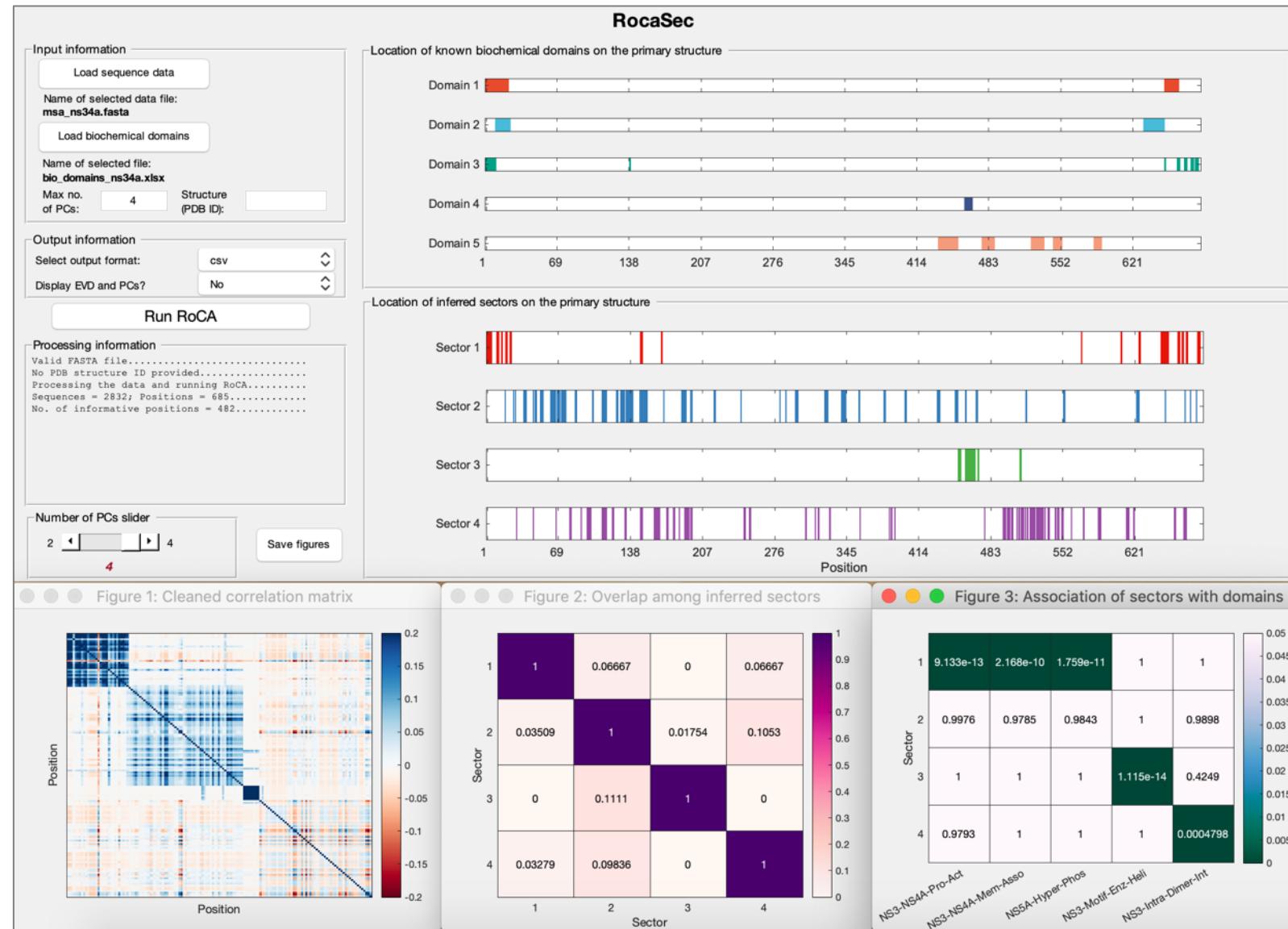
P24-Intra-Pent-Int



P7-Zinc-Finger

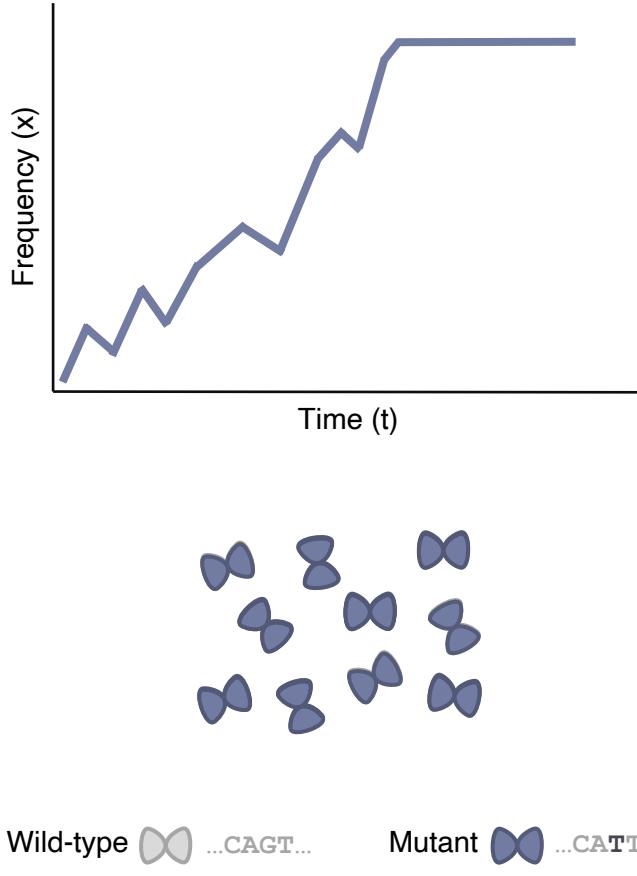


# RocaNet: A standalone GUI-based package for robust co-evolutionary analysis of proteins

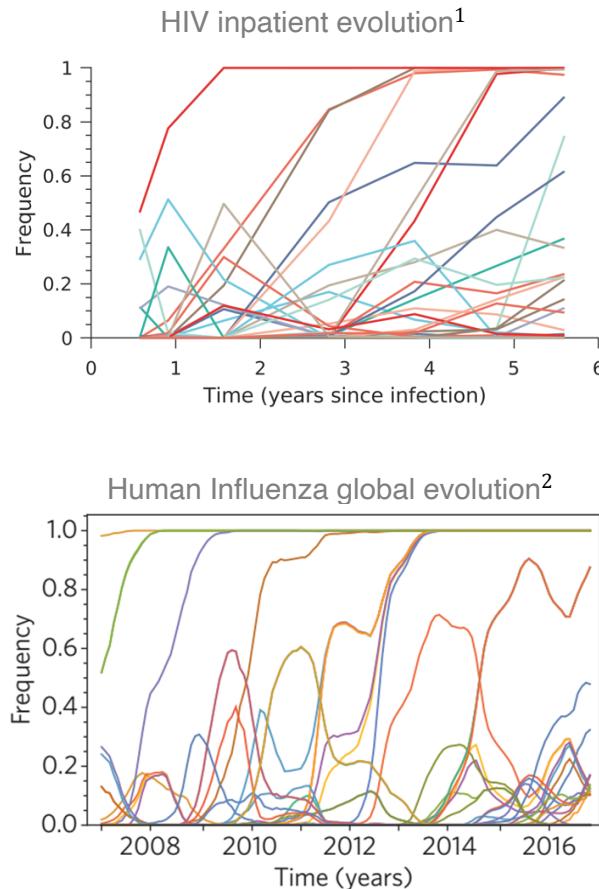


# Inferring fitness based on evolutionary histories

## Evolutionary history



## Real data



## Model: Wright-Fisher dynamics in the diffusion limit

**Assumption:** Fitness effects are additive

Evolution of mutant frequencies  $\underline{x} = \{x_1, x_2, \dots, x_L\}$  follows a **Fokker-Planck** (diffusion) equation

**Drift term:** expected change in mutant frequencies

$$d_i = x_i(1 - x_i)s_i + \sum_{i \neq j} (x_{ij} - x_i x_j)s_j + (1 - 2x_i)\mu$$

Selection      Linked selection      Mutation

↑                  ↑                  ↑

Mutant frequency    Selection coefficient    Double mutant frequency    Mutation probability

**Diffusion term:** characterizes fluctuations due to the stochasticity of replication

$$c_{ij} = \begin{cases} x_i(1 - x_i)/N & i = j \\ (x_{ij} - x_i x_j)/N & i \neq j \end{cases}$$

<sup>1</sup>Zanini, Fabio, et al. "Population genomics of intrapatient HIV-1 evolution." *Elife* 4 (2015): e11282.

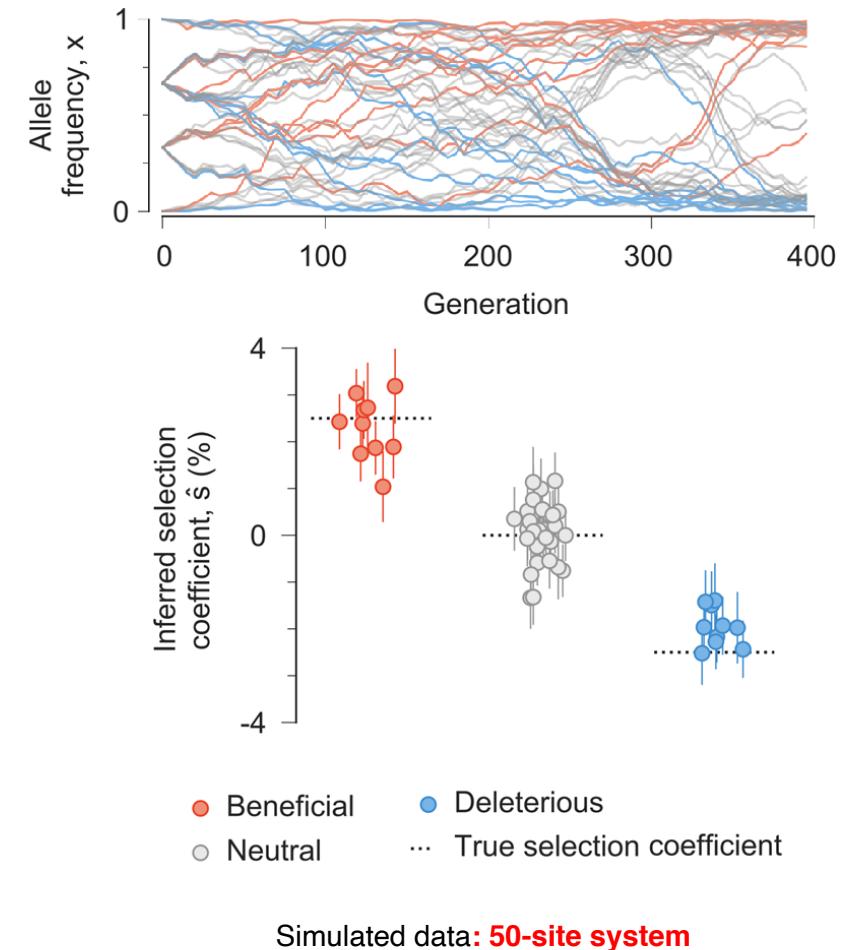
<sup>2</sup>Lässig, Michael, Ville Mustonen, and Aleksandra M. Walczak. "Predicting evolution." *Nature Ecology & Evolution* 1 (2017): 0077.

# Marginal path likelihood (MPL) estimate

- ▶ Evolutionary path  $X = \{\underline{x}(t_0), \underline{x}(t_1), \dots, \underline{x}(t_K)\}$
- ▶ Path integral --- probability of the evolutionary path  
 $P(X|s)$
- ▶ Maximum a posteriori solution

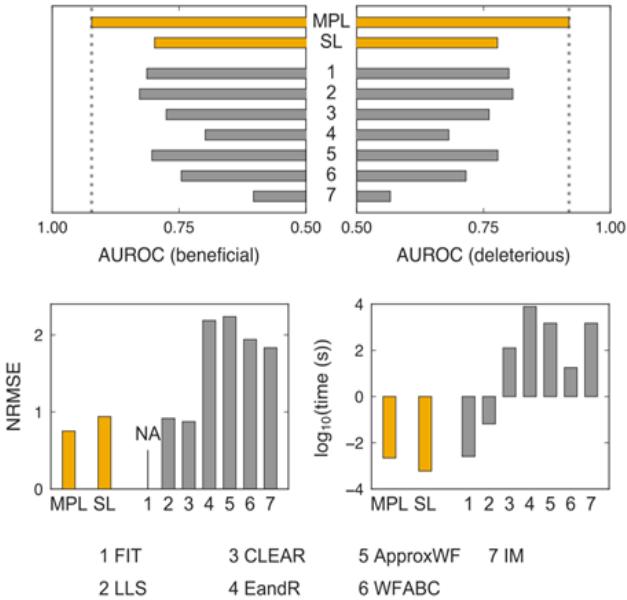
$$\hat{s}_i = \sum_{j=1}^L \left[ \left( \sum_{k=0}^{K-1} C(t_k) \Delta t \right) + \gamma I \right]_{ij}^{-1} \left[ x_j(t_K) - x_j(t_0) - \mu \sum_{k=0}^{K-1} \Delta t (1 - 2x_j(t_k)) \right]$$

Linkage effects
Change in frequency
Mutational flux



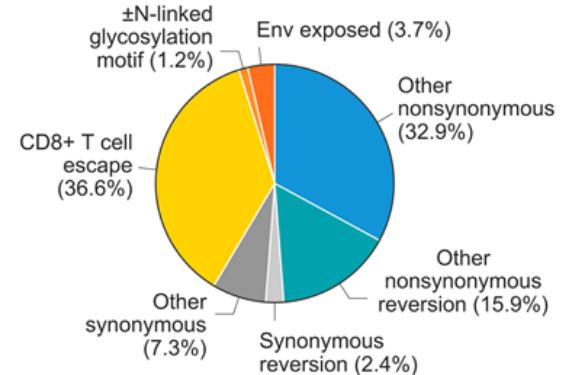
# Results

## Comparison with other methods

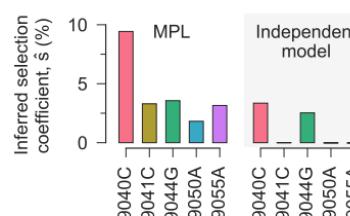
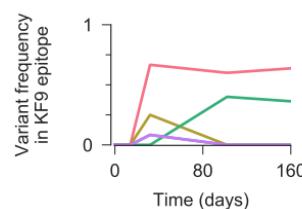


Simulated data: **50-site system**

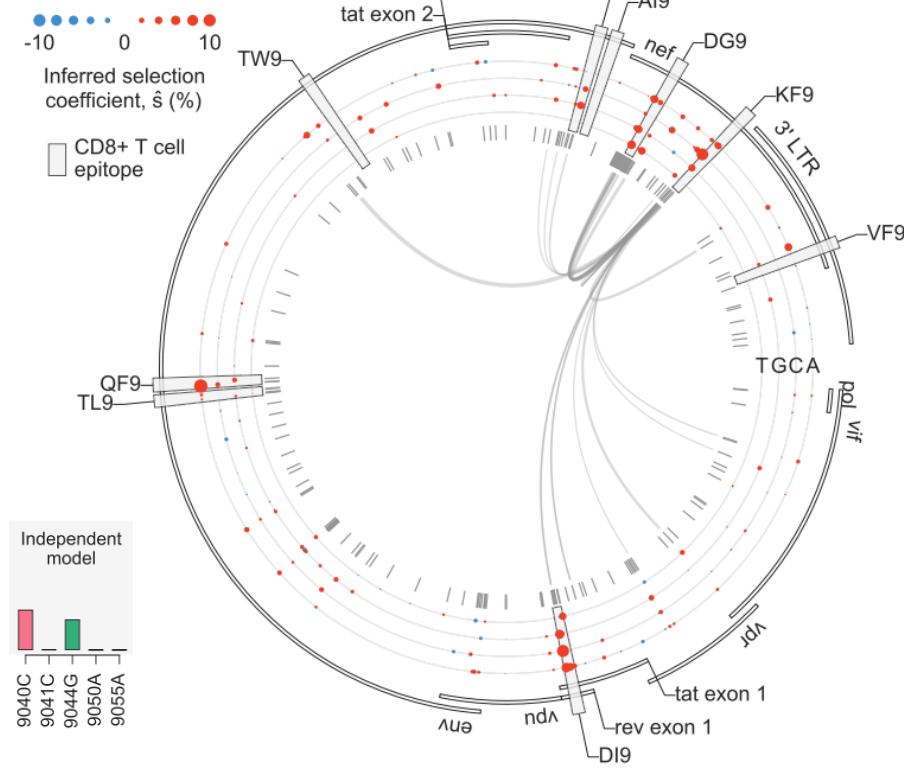
## Analysis of HIV half-genome longitudinal data of 14 individuals



Patterns of **strong selection:**  
Top 1% selection coefficients



Clonal interference in **KF9** epitope of patient **CH77**



Linkage patterns in patient **CH77**

# Acknowledgements

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**Berkeley**

Karthik Shekhar

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